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The goal of this chapter is to learn how to plan and conduct a *Production Process Characterization Study* (PPC) on manufacturing processes. We will learn how to model manufacturing processes and use these models to design a data collection scheme and to guide data analysis activities. We will look in detail at how to analyze the data collected in characterization studies and how to interpret and report the results. The accompanying <u>Case Studies</u> provide detailed examples of several process characterization studies.

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 - 1. Definition
 - 2. <u>Uses</u>
 - 3. Terminology/Concepts
 - 4. PPC Steps
- 3. Data Collection
 - 1. Set Goals
 - 2. <u>Model the Process</u>
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3.1. Introduction to Production Process Characterization

Overview The goal of this section is to provide an introduction to PPC. We will define PPC and the terminology used and discuss some of the possible Section uses of a PPC study. Finally, we will look at the steps involved in designing and executing a PPC study.

- Contents:
- Section 1
- 1. What is PPC?
- 2. What are PPC studies used for?
- 3. What terminology is used in PPC?
 - 1. Location, Spread and Shape
 - 2. Process Variability
 - 3. Propagating Error
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- 3. Production Process Characterization
- 3.1. Introduction to Production Process Characterization

3.1.1. What is PPC?

In PPC, we build data-based models	 Process characterization is an activity in which we: identify the key inputs and outputs of a process collect data on their behavior over the entire operating range estimate the steady-state behavior at optimal operating conditions and build models describing the parameter relationships across the operating range The result of this activity is a set of mathematical process models that we can use to monitor and improve the process.
This is a	This activity is typically a three-step process.
three-step	The Screening Step
process	In this phase we identify all possible significant process inputs and outputs and conduct a series of screening experiments in order to reduce that list to the key inputs and outputs. These experiments will also allow us to develop initial models of the relationships between those inputs and outputs.
	The Mapping Step
	In this step we map the behavior of the key outputs over their expected operating ranges. We do this through a series of more detailed experiments called Response Surface experiments.
	The Passive Step
	In this step we allow the process to run at nominal conditions and estimate the process stability and capability.
Not all of the steps need to be performed	The first two steps are only needed for new processes or when the process has undergone some significant engineering change. There are, however, many times throughout the life of a process when the third step is needed. Examples might be: initial process qualification, control chart development, after minor process adjustments, after schedule equipment maintenance, etc.



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3.1. Introduction to Production Process Characterization

3.1.2. What are PPC Studies Used For?

PPC is the core of any CI program Process characterization is an integral part of any continuous improvement program. There are many steps in that program for which process characterization is required. These might include:

- When process characterization is required
- when we are bringing a new process or tool into use.
- when we are bringing a tool or process back up after scheduled/unscheduled maintenance.
- when we want to compare tools or processes.
- when we want to check the health of our process during the monitoring phase.
- when we are troubleshooting a bad process.

The techniques described in this chapter are equally applicable to the other chapters covered in this Handbook. These include:

Process characterization techniques are applicable in other areas

- calibration
- process monitoring
- process improvement
- process/product comparison
- reliability





3.1. Introduction to Production Process Characterization

3.1.3. Terminology/Concepts

	There are just a few fundamental concepts needed for PPC. This section will review these ideas briefly and provide links to other sections in the Handbook where they are covered in more detail.
<u>Distribution(location,</u> <u>spread, shape)</u>	For basic data analysis, we will need to understand how to estimate location, spread and shape from the data. These three measures comprise what is known as the <i>distribution</i> of the data. We will look at both graphical and numerical techniques.
<u>Process variability</u>	We need to thoroughly understand the concept of process variability. This includes how variation explains the possible range of expected data values, the various classifications of variability, and the role that variability plays in process stability and capability.
Error propagation	We also need to understand how variation propagates through our manufacturing processes and how to decompose the total observed variation into components attributable to the contributing sources.
<u>Populations and</u> <u>sampling</u>	It is important to have an understanding of the various issues related to sampling. We will define a <i>population</i> and discuss how to acquire representative random samples from the population of interest. We will also discuss a useful formula for estimating the number of observations required to answer specific questions.
<u>Modeling</u>	For modeling, we will need to know how to identify important factors and responses. We will also need to know how to graphically and quantitatively build models of the relationships between the factors and responses.

Experiments

Finally, we will need to know about the basics of designed experiments including screening designs and response surface designs so that we can quantify these relationships. This topic will receive only a cursory treatment in this chapter. It is covered in detail in the process improvement chapter. However, examples of its use are in the case studies.

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3.1.3.1. Distribution (Location, Spread and Shape)



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3.1.3.1. Distribution (Location, Spread and Shape)

Distributions are characterized by location, spread and shape A fundamental concept in representing any of the outputs from a production process is that of a *distribution*. Distributions arise because any manufacturing process output will not yield the same value every time it is measured. There will be a natural scattering of the measured values about some central tendency value. This scattering about a central value is known as a distribution. A distribution is characterized by three values:

Location

The location is the expected value of the output being measured. For a stable process, this is the value around which the process has stabilized.

Spread

The spread is the expected amount of variation associated with the output. This tells us the range of possible values that we would expect to see.

Shape

The shape shows how the variation is distributed about the location. This tells us if our variation is symmetric about the mean or if it is skewed or possibly multimodal.

A primary goal of PPC is to estimate the distributions of the process outputs One of the primary goals of a PPC study is to characterize our process outputs in terms of these three measurements. If we can demonstrate that our process is stabilized about a constant location, with a constant variance and a known stable shape, then we have a process that is both predictable and controllable. This is required before we can set up control charts or conduct experiments. Click on
each item toThe table below shows
measures of location, sread more
detailParameter

The table below shows the most common numerical and graphical measures of location, spread and shape.

Parameter	Numerical	Graphical
Location	Imean	scatter plot boxplot histogram
Spread	ITANOP	boxplot histogram
Shape	kurtosis	boxplot histogram probability plot



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3.1. Introduction to Production Process Characterization

3.1.3. Terminology/Concepts

3.1.3.2. Process Variability

 Variability
 All manufacturing and measurement processes exhibit variation. For example, when we take sample data on the output of a process, such as critical dimensions, oxide thickness, or resistivity, we observe that all the values are *NOT* the same. This results in a collection of observed values distributed about some location value. This is what we call spread or variability. We represent variability numerically with the variance calculation and graphically with a histogram.

How doesThe standard deviation (square root of the variance) gives insight into the spread of the data throughthethe use of what is known as the Empirical Rule. This rule (shown in the graph below) is:standardApproximately 60-78% of the data are within a distance of one standard deviation from the averagedescribe the $(\bar{X}-s, \bar{X}+s)$.spread ofApproximately 90-98% of the data are within a distance of two standard deviations from the
average ($\bar{X}-2s, \bar{X}+2s$).

More than 99% of the data are within a distance of three standard deviations from the average ($\bar{x}^{-3s}, \bar{x}^{+3s}$).



VariabilityThis observed variability is an accumulation of many different sources of variation that have
occurred throughout the manufacturing process. One of the more important activities of process
characterization is to identify and quantify these various sources of variation so that they may be
minimized.

There areThere are not only different sources of variation, but there are also different types of variation. Twoalsoimportant classifications of variation for the purposes of PPC are controlled variation anddifferentuncontrolled variation.typestypes

<u>Click here</u> CONTROLLED VARIATION

to see

examples

Variation that is characterized by a *stable* and consistent pattern of variation over time. This type of variation will be *random* in nature and will be exhibited by a uniform fluctuation about a constant level.

UNCONTROLLED VARIATION

Variation that is characterized by a pattern of variation that *changes* over time and hence is unpredictable. This type of variation will typically contain some structure.

StableThis concept of controlled/uncontrolled variation is important in determining if a process is stable.processesA process is deemed stable if it runs in a consistent and predictable manner. This means that theonly exhibitaverage process value is constant and the variability is controlled. If the variation is uncontrolled,controlledthen either the process average is changing or the process variation is changing or both. The firstvariationprocess in the example above is stable; the second is not.

In the course of process characterization we should endeavor to eliminate all sources of uncontrolled variation.

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3.1.3.2.1. Controlled/Uncontrolled Variation



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- 3.1.3.2. Process Variability

3.1.3.2.1. Controlled/Uncontrolled Variation

Two trend plots

The two figures below are two trend plots from two different oxide growth processes. Thirty wafers were sampled from each process: one per day over 30 days. Thickness at the center was measured on each wafer. The *x*-*axis* of each graph is the wafer number and the *y*-*axis* is the film thickness in angstroms.

Examples of"in control" and "out of control" processes

The first process is an example of a process that is "in control" with random fluctuation about a process location of approximately 990. The second process is an example of a process that is "out of control" with a process location trending upward after observation 20.







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- 3.1.3. Terminology/Concepts

3.1.3.3. Propagating Error

The variation we see can come from many sources When we estimate the variance at a particular process step, this variance is typically not just a result of the current step, but rather is an accumulation of variation from previous steps and from measurement error. Therefore, an important question that we need to answer in PPC is how the variation from the different sources accumulates. This will allow us to partition the total variation and assign the parts to the various sources. Then we can attack the sources that contribute the most.

How do IUsually we can model the contribution of the various sources of error topartition thethe total error through a simple linear relationship. If we have a simpleerror?linear relationship between two variables, say,

$$y = \mu + c y_1 + \beta y_2$$

then the variance associated with, y, is given by,

$$Var(y) = \alpha^{2}Var(y_{1}) + \beta^{2}Var(y_{2}) + 2\alpha\beta Cov(y_{1}y_{2})$$

If the variables are not correlated, then there is no covariance and the last term in the above equation drops off. A good example of this is the case in which we have both process error and measurement error. Since these are usually independent of each other, the total observed variance is just the sum of the variances for process and measurement. Remember to never add standard deviations, we must add variances.

How do I calculate the individual components? Of course, we rarely have the individual components of variation and wish to know the total variation. Usually, we have an estimate of the overall variance and wish to break that variance down into its individual components. This is known as *components of variance* estimation and is dealt with in detail in the <u>analysis of variance</u> page later in this chapter.



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3.1.3.4. Populations and Sampling

We take samples from a target population and make inferences	In survey sampling, if you want to know what everyone thinks about a particular topic, you can just ask everyone and record their answers. Depending on how you define the term, everyone (all the adults in a town, all the males in the USA, etc.), it may be impossible or impractical to survey everyone. The other option is to survey a small group (Sample) of the people whose opinions you are interested in (Target Population), record their opinions and use that information to make inferences about what everyone thinks. Opinion pollsters have developed a whole body of tools for doing just that and many of those tools apply to manufacturing as well. We can use these sampling techniques to take a few measurements from a process and make statements about the behavior of that process.
Facts about a sample are not necessarily facts about a population	If it weren't for process variation we could just take one sample and everything would be known about the target population. Unfortunately this is never the case. We cannot take facts about the sample to be facts about the population. Our job is to reach appropriate conclusions about the population despite this variation. The more observations we take from a population, the more our sample data resembles the population. When we have reached the point at which facts about the sample are reasonable approximations of facts about the population, then we say the sample is adequate.
Four	Adequacy of a sample depends on the following four attributes:

- attributes of samples
- Representativeness of the sample (is it random?)
 - Size of the sample
 - Variability in the population
 - Desired precision of the estimates

We will learn about choosing representative samples of adequate size in the section on <u>defining sampling plans</u>.



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3.1.3.5. Process Models

Black box model and fishbone diagram	As we will see in Section 3 of this chapter, one of the first steps in PPC is to model the process that is under investigation. Two very useful tools for doing this are the <i>black-box</i> model and the <i>fishbone diagram</i> .
We use the black-box model to describe	We can use the simple <i>black-box</i> model, shown below, to describe most of the tools and processes we will encounter in PPC. The process will be stimulated by inputs. These inputs can either be controlled (such as recipe or machine settings) or uncontrolled (such as humidity, operators, power fluctuations, etc.). These inputs interact with our process

as number over fluctuations, etc.). These inputs interact with our process our and produce outputs. These outputs are usually some characteristic of our process that *processes* we can measure. The measurable inputs and outputs can be sampled in order to observe and understand how they behave and relate to each other.

Diagram of the black box model



These inputs and outputs are also known as Factors and Responses, respectively.

Factors

Observed inputs used to explain response behavior (also called explanatory variables). Factors may be fixed-level controlled inputs or sampled uncontrolled inputs.

Responses

Sampled process outputs. Responses may also be functions of sampled outputs such as average thickness or uniformity.

Factors We further categorize factors and responses according to their *Variable Type*, which indicates the amount of information they contain. As the name implies, this classification and is useful for data modeling activities and is critical for selecting the proper analysis Responses technique. The table below summarizes this categorization. The types are listed in order are further of the amount of information they contain with Measurement containing the most classified information and Nominal containing the least. by variable

type

describing the different variable	Туре	Description	Example
	Measurement	discrete/continuous, order is important, infinite range	particle count, oxide thickness, pressure, temperature
	Ordinal	discrete, order is important, finite range	run #, wafer #, site, bin
	Nominal	discrete, no order, very few possible values	good/bad, bin, high/medium/low, shift, operator

Fishbone diagrams help to decompose complexity We can use the fishbone diagram to further refine the modeling process. Fishbone diagrams are very useful for decomposing the complexity of our manufacturing processes. Typically, we choose a process characteristic (either Factors or Responses) and list out the general categories that may influence the characteristic (such as material, machine method, environment, etc.), and then provide more specific detail within each category. Examples of how to do this are given in the section on <u>Case Studies.</u>

Sample fishbone diagram











3.1.3.6. Experiments and Experimental Design



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- 3.1.3. Terminology/Concepts

3.1.3.6. Experiments and Experimental Design

Factors and responses	Besides just observing our processes for evidence of stability and capability, we quite often want to know about the relationships between the various Factors and Responses .
We look for correlations	There are generally two types of relationships that we are interested in for purposes of PPC. They are:
and causal	Correlation
relationships	Two variables are said to be correlated if an observed change in the level of one variable is accompanied by a change in the level of another variable. The change may be in the same direction (positive correlation) or in the opposite direction (negative correlation).
	Causality
	There is a causal relationship between two variables if a change in the level of one variable causes a change in the other variable.
	Note that correlation does not imply causality. It is possible for two variables to be associated with each other without one of them causing the observed behavior in the other. When this is the case it is usually because there is a third (possibly unknown) causal factor.
Our goal is to find causal relationships	Generally, our ultimate goal in PPC is to find and quantify causal relationships. Once this is done, we can then take advantage of these relationships to improve and control our processes.
Find correlations and then try to establish causal relationships	Generally, we first need to find and explore correlations and then try to establish causal relationships. It is much easier to find correlations as these are just properties of the data. It is much more difficult to prove causality as this additionally requires sound engineering judgment. There is a systematic procedure we can use to accomplish this in an efficient manner. We do this through the use of designed experiments.

First we screen, then we build models	When we have many potential factors and we want to see which ones are correlated and have the potential to be involved in causal relationships with the responses, we use <u>screening designs</u> to reduce the number of candidates. Once we have a reduced set of influential factors, we can use <u>response surface designs</u> to model the causal relationships with the responses across the operating range of the process factors.
Techniques discussed in process improvement chapter	The techniques are covered in detail in the process improvement section and will not be discussed much in this chapter. Examples of how the techniques are used in PPC are given in the <u>Case Studies</u> .



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3.1.4. PPC Steps

Follow theseThe primary activity of a PPC is to collect and analyze data so that we4 steps tomay draw conclusions about and ultimately improve our productionensureprocesses. In many industrial applications, access to production facilitiesefficient usefor the purposes of conducting experiments is very limited. Thus weof resourcesmust be very careful in how we go about these activities so that we can
be sure of doing them in a cost-effective manner.

Step 1: Plan The most important step by far is the planning step. By faithfully executing this step, we will ensure that we only collect data in the most efficient manner possible and still support the goals of the PPC. Planning should generate the following:

- a statement of the goals
- a descriptive process model (a list of process inputs and outputs)
- a description of the sampling plan (including a description of the procedure and settings to be used to run the process during the study with clear assignments for each person involved)
- a description of the method of data collection, tasks and responsibilities, formatting, and storage
- an outline of the data analysis

All decisions that affect how the characterization will be conducted should be made during the planning phase. The process characterization should be conducted according to this plan, with all exceptions noted.

Step 2:Data collection is essentially just the execution of the sampling plan partCollectof the previous step. If a good job were done in the planning step, then
this step should be pretty straightforward. It is important to execute to
the plan as closely as possible and to note any exceptions.

Step 3:This is the combination of quantitative (regression, ANOVA,Analyze andcorrelation, etc.) and graphical (histograms, scatter plots, box plots, etc.)interpretanalysis techniques that are applied to the collected data in order to
accomplish the goals of the PPC.

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Step 4:	Reporting is an important step that should not be overlooked. By
Report	creating an informative report and archiving it in an accessible place, we can ensure that others have access to the information generated by the PPC. Often, the work involved in a PPC can be minimized by using the results of other, similar studies. Examples of PPC reports can be found in the <u>Case Studies</u> section.
Further information	The planning and data collection steps are described in detail in the <u>data</u> <u>collection section</u> . The analysis and interpretation steps are covered in detail in the <u>analysis section</u> . Examples of the reporting step can be seen in the <u>Case Studies</u> .

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3. Production Process Characterization

3.2. Assumptions / Prerequisites

Primary goal is to *identify and* quantify sources of variation

The primary goal of PPC is to identify and quantify sources of variation. Only by doing this will we be able to define an effective plan for variation reduction and process improvement. Sometimes, in order to achieve this goal, we must first build mathematical/statistical models of our processes. In these models we will identify influential factors and the responses on which they have an effect. We will use these models to understand how the sources of variation are influenced by the important factors. This subsection will review many of the modeling tools we have at our disposal to accomplish these tasks. In particular, the models covered in this section are linear models, Analysis of Variance (ANOVA) models and discrete models.

Contents: Section 2	 <u>General Assumptions</u> <u>Continuous Linear</u>
	3. Analysis of Variance
	1. <u>One-Way</u>
	2. <u>Crossed</u>
	3. <u>Nested</u>
	4. <u>Discrete</u>

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- 3. Production Process Characterization
- 3.2. Assumptions / Prerequisites

3.2.1. General Assumptions

Assumption:In orprocess is sumthereof a systematicbe mcomponent andmoda randomcomcomponentpartsystemsystem

In order to employ the modeling techniques described in this section, there are a few assumptions about the process under study that must be made. First, we must assume that the process can adequately be modeled as the sum of a systematic component and a random component. The systematic component is the mathematical model part and the random component is the error or noise present in the system. We also assume that the systematic component is fixed over the range of operating conditions and that the random component has a constant location, spread and distributional form.

Assumption: data used to fit these models are representative of the process being modeled Finally, we assume that the data used to fit these models are representative of the process being modeled. As a result, we must additionally assume that the measurement system used to collect the data has been studied and proven to be capable of making measurements to the desired precision and accuracy. If this is not the case, refer to the <u>Measurement Capability Section</u> of this Handbook.

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3.2. Assumptions / Prerequisites

3.2.2. Continuous Linear Model

Description The continuous linear model (CLM) is probably the most commonly used model in PPC. It is applicable in many instances ranging from simple control charts to response surface models.

The CLM is a mathematical function that relates explanatory variables (either discrete or continuous) to a single continuous response variable. It is called linear because the coefficients of the terms are expressed as a linear sum. The terms themselves do not have to be linear.

Model The general form of the CLM is:

$$y = a_0 + \sum_{i=1}^p a_i f(x_i) + e$$

This equation just says that if we have p explanatory variables then the response is modeled by a constant term plus a sum of functions of those explanatory variables, plus some random error term. This will become clear as we look at some examples below.

- *Estimation* The coefficients for the parameters in the CLM are estimated by the method of least squares. This is a method that gives estimates which minimize the sum of the squared distances from the observations to the fitted line or plane. See the chapter on <u>Process Modeling</u> for a more complete discussion on estimating the coefficients for these models.
- *Testing* The tests for the CLM involve testing that the model as a whole is a good representation of the process and whether any of the coefficients in the model are zero or have no effect on the overall fit. Again, the details for testing are given in the chapter on <u>Process Modeling</u>.
- Assumptions For estimation purposes, there are no additional assumptions necessary for the CLM beyond those stated in the <u>assumptions</u> section. For testing purposes, however, it is necessary to assume that the error term is adequately modeled by a Gaussian distribution.

- Uses The CLM has many uses such as building predictive process models over a range of process settings that exhibit linear behavior, <u>control charts</u>, <u>process</u> capability, <u>building models from the data produced by designed</u> experiments, and building response surface models for automated process control applications.
- *Examples* Shewhart Control Chart The simplest example of a very common usage of the CLM is the underlying model used for Shewhart control charts. This model assumes that the process parameter being measured is a constant with additive Gaussian noise and is given by:

Diffusion Furnace - Suppose we want to model the average wafer sheet resistance as a function of the location or zone in a furnace tube, the temperature, and the anneal time. In this case, let there be 3 distinct zones (front, center, back) and temperature and time are continuous explanatory variables. This model is given by the CLM:

$$y=a_0+\left\{egin{array}{cc} a_1 & ext{if front} \ a_2+a_4temp+a_5time+e & ext{if center} \ a_3 & ext{if back} \end{array}
ight.$$

Diffusion Furnace (cont.) - Usually, the fitted line for the average wafer sheet resistance is not straight but has some curvature to it. This can be accommodated by adding a quadratic term for the time parameter as follows:

$$y=a_0+\left\{egin{array}{cc} a_1 & ext{if front} \ a_2+a_4temp+a_5time+a_6time^2e & ext{if center} \ a_3 & ext{if back} \end{array}
ight.$$

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<u>Production Process Characterization</u>
 Assumptions / Prerequisites

3.2.3. Analysis of Variance Models (ANOVA)

ANOVA allows us to compare the effects of multiple levels of multiple factors	One of the most common analysis activities in PPC is comparison. We often compare the performance of similar tools or processes. We also compare the effect of different treatments such as recipe settings. When we compare two things, such as two tools running the same operation, we use <u>comparison techniques</u> . When we want to compare multiple things, like multiple tools running the same operation or multiple tools with multiple operators running the same operation, we turn to ANOVA techniques to perform the analysis.
ANOVA splits the data into components	The easiest way to understand ANOVA is through a concept known as value splitting. ANOVA splits the observed data values into components that are attributable to the different levels of the factors. Value splitting is best explained by example.
Example: Turned Pins	The simplest example of value splitting is when we just have one level of one factor. Suppose we have a turning operation in a machine shop

of one factor. Suppose we have a turning operation in a machine shop where we are turning pins to a diameter of .125 +/- .005 inches. Throughout the course of a day we take five samples of pins and obtain the following measurements: .125, .127, .124, .126, .128.

We can split these data values into a common value (mean) and residuals (what's left over) as follows:



From these tables, also called overlays, we can easily calculate the location and spread of the data as follows:

mean = .126

std. deviation = .0016.

Other layouts While the above example is a trivial structural layout, it illustrates how we can split data values into its components. In the next sections, we will look at more complicated structural layouts for the data. In particular we will look at multiple levels of one factor (<u>One-Way</u> <u>ANOVA</u>) and multiple levels of two factors (Two-Way ANOVA) where the factors are <u>crossed</u> and <u>nested</u>.

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- 3. Production Process Characterization
- 3.2. <u>Assumptions / Prerequisites</u>

3.2.3. Analysis of Variance Models (ANOVA)

3.2.3.1. One-Way ANOVA

Description We say we have a one-way layout when we have a single factor with several levels and multiple observations at each level. With this kind of layout we can calculate the mean of the observations within each level of our factor. The residuals will tell us about the variation within each level. We can also average the means of each level to obtain a grand mean. We can then look at the deviation of the mean of each level from the grand mean to understand something about the level effects. Finally, we can compare the variation within levels to the variation across levels. Hence the name analysis of variance.

Model It is easy to model all of this with an equation of the form:

 $y_{ij} = m + a_i + e_{ij}$

This equation indicates that the *jth* data value, from level *i*, is the sum of three components: the common value (grand mean), the level effect (the deviation of each level mean from the grand mean), and the residual (what's left over).

EstimationEstimation for the one-way layout can be performed one of two ways.click here toFirst, we can calculate the total variation, within-level variation and
across-level variation. These can be summarized in a table as shown
below and tests can be made to determine if the factor levels are
significant. The value splitting example illustrates the calculations
involved.

ANOVA *table for* **Degrees of** Source **Sum of Squares Mean Square** one-way Freedom case Factor I-1 levels /(I-1) $\sum \sum e_{ij}^2$ I(J-1) residuals /I(J-1) corrected total $\sum \sum y_{ij}^2 - IJm^2$ IJ-1

In general, the ANOVA table for the one-way case is given by:

Level effects must sum to zero

The other way is through the use of <u>CLM</u> techniques. If you look at the model above you will notice that it is in the form of a CLM. The only problem is that the model is saturated and no unique solution exists. We overcome this problem by applying a constraint to the model. Since the level effects are just deviations from the grand mean, they must sum to zero. By applying the constraint that the level effects must sum to zero, we can now obtain a unique solution to the CLM equations. Most analysis programs will handle this for you automatically. See the chapter on Process Modeling for a more complete discussion on estimating the coefficients for these models.

Testing The testing we want to do in this case is to see if the observed data support the hypothesis that the levels of the factor are significantly different from each other. The way we do this is by comparing the within-level variance to the between-level variance.

> If we assume that the observations within each level have the same variance, we can calculate the variance within each level and pool these together to obtain an estimate of the overall population variance. This works out to be the mean square of the residuals.

Similarly, if there really were no level effect, the mean square across levels would be an estimate of the overall variance. Therefore, if there really were no level effect, these two estimates would be just two different ways to estimate the same parameter and should be close numerically. However, if there is a level effect, the level mean square will be higher than the residual mean square.

It can be shown that given the assumptions about the data stated below, the ratio of the level mean square and the residual mean square follows an <u>F distribution</u> with degrees of freedom as shown in the ANOVA table. If the F-value is significant at a given level of confidence (greater than the cut-off value in a F-Table), then there is a level effect present in the data.

- Assumptions For estimation purposes, we assume the data can adequately be modeled as the sum of a deterministic component and a random component. We further assume that the fixed (deterministic) component can be modeled as the sum of an overall mean and some contribution from the factor level. Finally, it is assumed that the random component can be modeled with a Gaussian distribution with fixed location and spread.
- *Uses* The one-way ANOVA is useful when we want to compare the effect of multiple levels of one factor and we have multiple observations at each level. The factor can be either discrete (different machine, different plants, different shifts, etc.) or continuous (different gas flows, temperatures, etc.).
- *Example* Let's extend the <u>machining example</u> by assuming that we have five different machines making the same part and we take five random samples from each machine to obtain the following diameter data:

Machine					
<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	
.125	.118	.123	.126	.118	
.127	.122	.125	.128	.129	
.125	.120	.125	.126	.127	
.126	.124	.124	.127	.120	
.128	.119	.126	.129	.121	

Analyze Using ANOVA software or the techniques of the <u>value-splitting</u> example, we summarize the data into an ANOVA table as follows:

Source	Sum of Squares	Degrees of Freedom	Mean Square	F-value
Factor levels	.000137	4	.000034	4.86 > 2.87
residuals	.000132	20	.000007	
corrected total	.000269	24		

Test	By dividing the Factor-level mean square by the residual mean square, we obtain a F-value of 4.86 which is greater than the cut-off value of 2.87 for the F-distribution at 4 and 20 degrees of freedom and 95% confidence. Therefore, there is sufficient evidence to reject the hypothesis that the levels are all the same.					
Conclusion	From the analysis of these data we can conclude that the factor "machine" has an effect. There is a statistically significant difference in the pin diameters across the machines on which they were manufactured.					
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- 3.2.3. Analysis of Variance Models (ANOVA)
- 3.2.3.1. One-Way ANOVA

3.2.3.1.1. One-Way Value-Splitting

Example

Let's use the data from the machining example to illustrate how to use the techniques of value-splitting to break each data value into its component parts. Once we have the component parts, it is then a trivial matter to calculate the sums of squares and form the F-value for the test.

Machine					
<u>1</u>	2	<u>3</u>	<u>4</u>	<u>5</u>	
.125	.118	.123	.126	.118	
.127	.122	.125	.128	.129	
.125	.120	.125	.126	.127	
.126	.124	.124	.127	.120	
.128	.119	.126	.129	.121	

Calculate level-means Remember from our model, $y_{ij} = m + a_i + e_{ij}$, we say each observation is the sum of a common value, a level effect and a residual value. Value-splitting just breaks each observation into its component parts. The first step in value-splitting is to calculate the mean values (rounding to the nearest thousandth) within each machine to get the level means.

Machine						
$\boxed{\underline{1}} \ \underline{2} \ \underline{3} \ \underline{4} \ \underline{5}$						
.1262 .1206 .1246 .1272 .123						

Sweep levelWe can then sweep (subtract the level mean from each associated datameansvalue) the means through the original data table to get the residuals:

Machine						
<u>1</u>	2	<u>3</u>	<u>4</u>	<u>5</u>		
0012	0026	0016	0012	005		
.0008	.0014	.0004	.0008	.006		
0012	0006	.0004	0012	.004		
0002	.0034	0006	0002	003		
.0018	0016	.0014	.0018	002		

Calculate The next step is to calculate the grand mean from the individual machine means as:

Grand
Mean
.12432

Machine						
<u>1</u>	$\boxed{1} 2 3 4 5$					
.0018800372 .00028 .0028800132						

It is easy to verify that the original data table can be constructed by adding the overall mean, the machine effect and the appropriate residual.

CalculateNow that we have the data values split and the overlays created, the nextANOVAstep is to calculate the various values in the One-Way ANOVA table.valuesWe have three values to calculate for each overlay. They are the sums of
squares, the degrees of freedom, and the mean squares.

Total sum ofThe total sum of squares is calculated by summing the squares of all the
data values and subtracting from this number the square of the grand
mean times the total number of data values. We usually don't calculate
the mean square for the total sum of squares because we don't use this
value in any statistical test.

Residual sum of squares, degrees of freedom and mean square	The residual sum of squares is calculated by summing the squares of the residual values. This is equal to .000132. The degrees of freedom is the number of unconstrained values. Since the residuals for each level of the factor must sum to zero, once we know four of them, the last one is determined. This means we have four unconstrained values for each level, or 20 degrees of freedom. This gives a mean square of .000007.
Level sum of squares, degrees of freedom and mean square	Finally, to obtain the sum of squares for the levels, we sum the squares of each value in the level effect overlay and multiply the sum by the number of observations for each level (in this case 5) to obtain a value of .000137. Since the deviations from the level means must sum to zero, we have only four unconstrained values so the degrees of freedom for level effects is 4. This produces a mean square of .000034.
Calculate F-value	The last step is to calculate the F-value and perform the test of equal level means. The F- value is just the level mean square divided by the residual mean square. In this case the F-value=4.86. If we look in an F-table for 4 and 20 degrees of freedom at 95% confidence, we see that the critical value is 2.87, which means that we have a significant result and that there is thus evidence of a strong machine effect. By looking at the level-effect overlay we see that this is driven by machines 2 and 4.

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3.2.3. Analysis of Variance Models (ANOVA)

3.2.3.2. Two-Way Crossed ANOVA

- *Description* When we have two factors with at least two levels and one or more observations at each level, we say we have a two-way layout. We say that the two-way layout is crossed when every level of Factor A occurs with every level of Factor B. With this kind of layout we can estimate the effect of each factor (Main Effects) as well as any <u>interaction</u> between the factors.
- *Model* If we assume that we have K observations at each combination of I levels of Factor A and J levels of Factor B, then we can model the two-way layout with an equation of the form:

$$y_{ijk} = m + a_i + b_j + (ab)_{ij} + e_{ijk}$$

This equation just says that the *kth* data value for the *jth* level of Factor B and the *ith* level of Factor A is the sum of five components: the common value (grand mean), the level effect for Factor A, the level effect for Factor B, the interaction effect, and the residual. Note that (ab) does not mean multiplication; rather that there is interaction between the two factors.

Estimation Like the one-way case, the estimation for the two-way layout can be done either by calculating the variance components or by using <u>CLM</u> techniques.

Click here
for the valueFor the variance components methods we display the data in a two
dimensional table with the levels of Factor A in columns and the levels
of Factor B in rows. The replicate observations fill each cell. We can
sweep out the common value, the row effects, the column effects, the
interaction effects and the residuals using value-splitting techniques.
Sums of squares can be calculated and summarized in an ANOVA table
as shown below.

Source	Sum of Squares	Degrees of Freedom	Mean Square
rows	$JK\sum a_i^2$	I-1	$JK \sum a_{i/(I-1)}^2$
columns	$IK \sum b_j^2$	J-1	$IK \sum b_{j}^{2} b_{j/(J-1)}$
interaction	$K\sum \sum (ab)_{ij}^2$	(I-1)(J-1)	$K\sum \sum \left(ab\right)^2_{ij}$
residuals	$\sum \sum \sum e_{ijk}^2$	IJ(K-1)	$\sum \sum \sum e_{ijk/\text{IJ}(\text{K-1})}^2$
corrected total	$\sum \sum y_{ij}^2 - IJm^2$	IJK-1	

We can use <u>CLM</u> techniques to do the estimation. We still have the problem that the model is <u>saturated</u> and no unique solution exists. We overcome this problem by applying the constraints to the model that the two main effects and interaction effects each sum to zero.

- *Testing* Like testing in the <u>one-way case</u>, we are testing that two main effects and the interaction are zero. Again we just form a ratio of each main effect mean square and the interaction mean square to the residual mean square. If the assumptions stated below are true then those ratios follow an F-distribution and the test is performed by comparing the F-ratios to values in an F-table with the appropriate degrees of freedom and confidence level.
- *Assumptions* For estimation purposes, we assume the data can be adequately modeled as described in the model above. It is assumed that the random component can be modeled with a Gaussian distribution with fixed location and spread.
- *Uses* The two-way crossed ANOVA is useful when we want to compare the effect of multiple levels of two factors and we can combine every level of one factor with every level of the other factor. If we have multiple observations at each level, then we can also estimate the effects of interaction between the two factors.

Example Let's extend the <u>one-way machining example</u> by assuming that we want to test if there are any differences in pin diameters due to different types of coolant. We still have five different machines making the same part and we take five samples from each machine for each coolant type to obtain the following data:

	Machine						
	1	2	<u>3</u>	<u>4</u>	<u>5</u>		
	.125	.118	.123	.126	.118		
Coolant	.127	.122	.125	.128	.129		
A	.125	.120	.125	.126	.127		
	.126	.124	.124	.127	.120		
	.128	.119	.126	.129	.121		
	.124	.116	.122	.126	.125		
Coolort	.128	.125	.121	.129	.123		
Coolant B	.127	.119	.124	.125	.114		
	.126	.125	.126	.130	.124		
	.129	.120	.125	.124	.117		

Analyze

For analysis details see the <u>crossed two-way value splitting example</u>. We can summarize the analysis results in an ANOVA table as follows:

Source	Sum of Squares	Degrees of Freedom	Mean Square	F-value
machine	.000303	4	.000076	8.8 > 2.61
coolant	.00000392	1	.00000392	.45 < 4.08
interaction	.00001468	4	.00000367	.42 < 2.61
residuals	.000346	40	.0000087	
corrected total	.000668	49		

Test By dividing the mean square for machine by the mean square for residuals we obtain an F-value of 8.8 which is greater than the cut-off value of 2.61 for 4 and 40 degrees of freedom and a confidence of 95%. Likewise the F-values for Coolant and Interaction, obtained by dividing their mean squares by the residual mean square, are less than their respective cut-off values.

Conclusion From the ANOVA table we can conclude that machine is the most important factor and is statistically significant. Coolant is not significant and neither is the interaction. These results would lead us to believe that some tool-matching efforts would be useful for improving this process.

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- 3.2.3. Analysis of Variance Models (ANOVA)
- 3.2.3.2. Two-Way Crossed ANOVA

3.2.3.2.1. Two-way Crossed Value-Splitting Example

Example: Coolant is completely crossed with machine The data table below is five samples each collected from five different lathes each running two different types of coolant. The measurement is the diameter of a turned pin.

		Machine							
	1	2	3	<u>4</u>	5				
			.123		J				
Coolant	.127	.122	.125	.128	.129				
A	.125	.120	.125	.126	.127				
	.126	.124	.124	.127	.120				
	.128	.119	.126	.129	.121				
	.124	.116	.122	.126	.125				
Coolont	.128	.125	.121	.129	.123				
Coolant B	.127	.119	.124	.125	.114				
	.126	.125	.126	.130	.124				
	.129	.120	.125	.124	.117				

For the crossed two-way case, the first thing we need to do is to sweep the cell means from the data table to obtain the residual values. This is shown in the tables below.

The first			Ν	Aachin	e	
step is to sweep out		<u>1</u>	2	3	4	<u>5</u>
the cell	A	.1262	.1206	.1246	.1272	.123
means to	B	.1268	.121	.1236	.1268	.1206
obtain the		0012	0026	0016	0012	005
residuals and means	Coolant	.0008	.0014	.0004	.0008	.006
and means	A	0012	0006	.0004	0012	.004
		0002	.0034	0006	0002	003
		.0018	0016	.0014	.0018	002
		0028	005	0016	0008	.0044
	Coolort	.0012	.004	0026	.0022	.0024
	Coolant B	.0002	002	.0004	0018	0066
		0008	.004	.0024	.0032	.0034
		.0022	001	.0014	0028	0036

Sweep the The next step is to sweep out the row means. This gives the table below. *row means*

		Machine						
		<u>1</u>	2	3	<u>4</u>	5		
A	.1243	.0019	0037	.0003	.0029	0013		
B	.1238	.003	0028	0002	.003	0032		

Sweep the
columnFinally, we sweep the column means to obtain the grand mean, row
(coolant) effects, column (machine) effects and the interaction effects.means

		Machine						
		<u>1</u> <u>2</u> <u>3</u> <u>4</u> <u>5</u>						
	.1241	.0025	0033	.00005	.003	0023		
A	.0003	0006	0005	.00025	.0000	.001		
B	0003	.0006	.0005	00025	.0000	001		

What do
these tablesBy looking at the table of residuals, we see that the residuals for coolant
B tend to be a little higher than for coolant A. This implies that there
may be more variability in diameter when we use coolant B. From the
effects table above, we see that machines 2 and 5 produce smaller pin
diameters than the other machines. There is also a very slight coolant
effect but the machine effect is larger. Finally, there also appears to be
slight interaction effects. For instance, machines 1 and 2 had smaller
diameters with coolant A but the opposite was true for machines 3,4 and
5.

Calculate sums of squares and mean squares

We can calculate the values for the ANOVA table according to the formulae in the table on the crossed two-way page. This gives the table
below. From the F-values we see that the machine effect is significant but the coolant and the interaction are not.

Source	Sums of Squares	Degrees of Freedom	Mean Square	F-value
Machine	.000303	4	.000076	8.8 > 2.61
Coolant	.00000392	1	.00000392	.45 < 4.08
Interaction	.00001468	4	.00000367	.42 < 2.61
Residual	.000346	40	.0000087	
Corrected Total	.000668	49		

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- 3. Production Process Characterization
- 3.2. <u>Assumptions / Prerequisites</u>

3.2.3. Analysis of Variance Models (ANOVA)

3.2.3.3. Two-Way Nested ANOVA

Description Sometimes, constraints prevent us from crossing every level of one factor with every level of the other factor. In these cases we are forced into what is known as a *nested* layout. We say we have a nested layout when fewer than all levels of one factor occur within each level of the other factor. An example of this might be if we want to study the effects of different machines and different operators on some output characteristic, but we can't have the operators change the machines they run. In this case, each operator is not crossed with each machine but rather only runs one machine.

Model If Factor B is nested within Factor A, then a level of Factor B can only occur within one level of Factor A and there can be no interaction. This gives the following model:

 $y_{ijk} = m + a_i + b_{j(i)} + e_{ijk}$

This equation indicates that each data value is the sum of a common value (grand mean), the level effect for Factor A, the level effect of Factor B nested Factor A, and the residual.

Estimation For a nested design we typically use variance components methods to perform the analysis. We can sweep out the common value, the row effects, the column effects and the residuals using <u>value-splitting</u> techniques. Sums of squares can be calculated and summarized in an ANOVA table as shown below.

Click here
for nestedIt is important to note that with this type of layout, since each level of one
factor is only present with one level of the other factor, we can't estimate
interaction between the two.value-
linitial

ANOVA table for nested case

Source	Sum of Squares	Degrees of Freedom	Mean Square
rows	$JK\sum a_i^2$	I-1	$JK \sum a_{i}^2$
columns	$IK \sum b_j^2$	I(J-1)	$IK \sum b_{j}^{2}$
residuals	$\sum \sum \sum e_{ijk}^2$	IJ(K-1)	$\sum \sum \sum e_{ijk/IJ(K-1)}^2$
corrected total	$\sum \sum y_{ij}^2 - IJm^2$	IJK-1	

As with the crossed layout, we can also use \underline{CLM} techniques. We still have the problem that the model is saturated and no unique solution exists. We overcome this problem by applying to the model the constraints that the two main effects sum to zero.

Testing We are testing that two main effects are zero. Again we just form a ratio of each main effect mean square to the residual mean square. If the assumptions stated below are true then those ratios follow an F-distribution and the test is performed by comparing the F-ratios to values in an F-table with the appropriate degrees of freedom and confidence level.

Assumptions For estimation purposes, we assume the data can be adequately modeled as described in the model above. It is assumed that the random component can be modeled with a Gaussian distribution with fixed location and spread.

Uses The two-way nested ANOVA is useful when we are constrained from combining all the levels of one factor with all of the levels of the other factor. These designs are most useful when we have what is called a random effects situation. When the levels of a factor are chosen at random rather than selected intentionally, we say we have a random effects model. An example of this is when we select lots from a production run, then select units from the lot. Here the units are nested within lots and the effect of each factor is random. *Example* Let's change the <u>two-way machining example</u> slightly by assuming that we have five different machines making the same part and each machine has two operators, one for the day shift and one for the night shift. We take five samples from each machine for each operator to obtain the following data:

		Machine							
	1	2	<u>3</u>	<u>4</u>	<u>5</u>				
	.125	.118	.123	.126	.118				
Operator	.127	.122	.125	.128	.129				
Day	.125	.120	.125	.126	.127				
	.126	.124	.124	.127	.120				
	.128	.119	.126	.129	.121				
	.124	.116	.122	.126	.125				
Onemator	.128	.125	.121	.129	.123				
Operator Night	.127	.119	.124	.125	.114				
	.126	.125	.126	.130	.124				
	.129	.120	.125	.124	.117				

Analyze For analysis details see the <u>nested two-way value splitting example.</u> We can summarize the analysis results in an ANOVA table as follows:

Source	Sum of Squares	Degrees of Freedom	Mean Square	F-value
Machine	.000303	4	.0000758	8.77 > 2.61
Operator(Machine)	.0000186	5	.00000372	.428 < 2.45
Residuals	.000346	40	.0000087	
Corrected Total	.000668	49		

Test By dividing the mean square for machine by the mean square for residuals we obtain an F-value of 8.5 which is greater than the cut-off value of 2.61 for 4 and 40 degrees of freedom and a confidence of 95%. Likewise the F-value for Operator(Machine), obtained by dividing its mean square by the residual mean square is less than the cut-off value of 2.45 for 5 and 40 degrees of freedom and 95% confidence.

Conclusion From the ANOVA table we can conclude that the Machine is the most important factor and is statistically significant. The effect of Operator nested within Machine is not statistically significant. Again, any improvement activities should be focused on the tools.

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3.2.3.3.1. Two-Way Nested Value-Splitting Example



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3.2.3.3. Two-Way Nested ANOVA

3.2.3.3.1. Two-Way Nested Value-Splitting Example

Example: **Operator** is nested within machine.

The data table below contains data collected from five different lathes, each run by two different operators. Note we are concerned here with the effect of operators, so the layout is nested. If we were concerned with shift instead of operator, the layout would be crossed. The measurement is the diameter of a turned pin.

Machina	Operator		S	ampl	e	
Machine	Operator	1	2	3	4	5
1	Day		.127			
	Night	.124	.128	.127	.126	.129
2	Day	.118	.122	.120	.124	.119
	Night	.116	.125	.119	.125	.120
3	Day	.123	.125	.125	.124	.126
5	Night	.122	.121	.124	.126	.125
Δ	Day		.128			
-	Night	.126	.129	.125	.130	.124
5	Day	.118	.129	.127	.120	.121
5	Night	.125	.123	.114	.124	.117

For the nested two-way case, just as in the crossed case, the first thing we need to do is to sweep the cell means from the data table to obtain the residual values. We then sweep the nested factor (Operator) and the top level factor (Machine) to obtain the table below.

Machine	Operator	Common	Machina	Operator		5	Sample)											
		Common	wiachine		<u><u>1</u></u>	2	3	<u>4</u>	<u>5</u>										
1	Day		.00246	0003	0012	.0008	0012	0002	.0018										
	Night		.00240	.0003	0028	.0012	.002	0008	.0022										
2	Day		00324	0002	0026	.0014	0006	.0034	0016										
	Night		00324	.0002	005	.004	002	.004	001										
3	Day	.12404	.00006	.0005	0016	.0004	.0004	0006	.0014										
5	Night	.12404	.00000	.00000	.00000	.00000	.00000	.00000	.00000	.00000	.00000	.00000	.00000	0005	0016	0026	.0004	.0024	.0014
4	Day		.00296	.0002	0012	.0008	0012	002	.0018										
	Night		.00290	0002	0008	.0022	0018	.0032	0028										
	Day			.0012	005	.006	.004	003	002										

5 Night002240012 .0044 .00240066 .003400
--

WhatBy looking at the residuals we see that machines 2 and 5 have the greatest variability.does thisThere does not appear to be much of an operator effect but there is clearly a strong machinetable telleffect.us?Use the strong machine

CalculateWe can calculate the values for the ANOVA table according to the formulae in the table on
the nested two-way page. This produces the table below. From the F-values we see that the
machine effect is significant but the operator effect is not. (Here it is assumed that both
factors are fixed).mean

squares

Source	Sums of Squares	Degrees of Freedom	Mean Square	F-value
Machine	.000303	4	.0000758	8.77 > 2.61
Operator(Machine)	.0000186	5	.00000372	.428 < 2.45
Residual	.000346	40	.0000087	
Corrected Total	.000668	49		

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- 3. Production Process Characterization
- 3.2. Assumptions / Prerequisites

3.2.4. Discrete Models

- Description There are many instances when we are faced with the analysis of discrete data rather than continuous data. Examples of this are yield (good/bad), speed bins (slow/fast/faster/fastest), survey results (favor/oppose), etc. We then try to explain the discrete outcomes with some combination of discrete and/or continuous explanatory variables. In this situation the modeling techniques we have learned so far (CLM and ANOVA) are no longer appropriate.
- Contingency
tableThere are two primary methods available for the analysis of discrete
response data. The first one applies to situations in which we have
discrete explanatory variables and discrete responses and is known as
Contingency Table Analysis. The model for this is covered in detail in
this section. The second model applies when we have both discrete and
continuous explanatory variables and is referred to as a Log-Linear
Model. That model is beyond the scope of this Handbook, but interested
readers should refer to the reference section of this chapter for a list of
useful books on the topic.
- ModelSuppose we have n individuals that we classify according to two
criteria, A and B. Suppose there are r levels of criterion A and s levels
of criterion B. These responses can be displayed in an $r \mathbf{x} s$ table. For
example, suppose we have a box of manufactured parts that we classify
as good or bad and whether they came from supplier 1, 2 or 3.

Now, each cell of this table will have a count of the individuals who fall into its particular combination of classification levels. Let's call this count N_{ij} . The sum of all of these counts will be equal to the total number of individuals, N. Also, each row of the table will sum to N_{i} and each column will sum to $N_{.j}$.

Under the assumption that there is no interaction between the two classifying variables (like the number of good or bad parts does not depend on which supplier they came from), we can calculate the counts we would expect to see in each cell. Let's call the expected count for any cell E_{ij} . Then the expected value for a cell is $E_{ij} = N_{i.} * N_{.j} / N$. All we need to do then is to compare the expected counts to the observed counts. If there is a consderable difference between the observed counts and the expected values, then the two variables interact in some way.

- *Estimation* The estimation is very simple. All we do is make a table of the observed counts and then calculate the expected counts as described above.
- *Testing* The test is performed using a Chi-Square goodness-of-fit test according to the following formula:

$$\chi^2 = \sum \sum \frac{(\text{observed} - \text{expected})^2}{\text{expected}}$$

where the summation is across all of the cells in the table.

Given the assumptions stated below, this statistic has approximately a chi-square distribution and is therefore compared against a chi-square table with (r-1)(s-1) degrees of freedom, with r and s as previously defined. If the value of the test statistic is less than the chi-square value for a given level of confidence, then the classifying variables are declared independent, otherwise they are judged to be dependent.

- Assumptions The estimation and testing results above hold regardless of whether the sample model is Poisson, multinomial, or product-multinomial. The chi-square results start to break down if the counts in any cell are small, say < 5.
- *Uses* The contingency table method is really just a test of interaction between discrete explanatory variables for discrete responses. The example given below is for two factors. The methods are equally applicable to more factors, but as with any interaction, as you add more factors the interpretation of the results becomes more difficult.
- *Example* Suppose we are comparing the yield from two manufacturing processes. We want want to know if one process has a higher yield.

Make table of counts

	Good	Bad	Totals
Process A	86	14	100
Process B	80	20	100
Totals	166	34	200

Table 1. Yields for two production processes

We obtain the expected values by the formula given above. This gives the table below.

Calculate expected counts

	Good	Bad	Totals
Process A	83	17	100
Process B	83	17	100
Totals	166	34	200

Table 2. Expected values for two production processes

Calculate chi-square statistic and compare to table value	degree of fr	are statistic is 1.276. Treedom and 90% confination not a (significant) dif	dence of 2.71. The	herefore, we c	
Conclusion		we conclude that there between the two proces	•	significant	
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3. Production Process Characterization

3.3. Data Collection for PPC

Start with The data collection process for PPC starts with careful planning. The planning consists of the definition of clear and concise goals, developing careful process models and devising a sampling plan. planning

Many things This activity of course ends without the actual collection of the data which is usually not as straightforward as it might appear. Many things can go can go wrong in the execution of the sampling plan. The problems can wrong in the be mitigated with the use of check lists and by carefully documenting all collection exceptions to the original sampling plan.

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data

1. Set Goals

2. Modeling Processes

- 1. Black-Box Models
- 2. Fishbone Diagrams
- 3. Relationships and Sensitivities
- 3. Define the Sampling Plan
 - 1. Identify the parameters, ranges and resolution
 - 2. Design sampling scheme
 - 3. Select sample sizes
 - 4. Design data storage formats
 - 5. Assign roles and responsibilities

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3. Production Process Characterization

3.3. Data Collection for PPC

3.3.1. Define Goals

State concise goals	The goal statement is one of the most important parts of the characterization plan. With clearly and concisely stated goals, the rest of the planning process falls naturally into place.
Goals usually defined in terms of key specifications	The goals are usually defined in terms of key specifications or manufacturing indices. We typically want to characterize a process and compare the results against these specifications. However, this is not always the case. We may, for instance, just want to quantify key process parameters and use our estimates of those parameters in some other activity like controller design or process improvement.
Example goal statements	 Click on each of the links below to see Goal Statements for each of the case studies. 1. <u>Furnace Case Study (Goal)</u> 2. <u>Machine Case Study (Goal)</u>





3. Production Process Characterization

3.3. Data Collection for PPC

3.3.2. Process Modeling

Identify influential parameters Process modeling begins by identifying all of the important factors and responses. This is usually best done as a team effort and is limited to the scope set by the goal statement.

Document with black-box models This activity is best documented in the form of a black-box model as seen in the figure below. In this figure all of the outputs are shown on the right and all of the controllable inputs are shown on the left. Any inputs or factors that may be observable but not controllable are shown on the top or bottom.



3.3.2. Process Modeling

Model

using

The next step is to model relationships of the previously identified factors and responses. In this step we choose a parameter and identify *relationships* all of the other parameters that may have an influence on it. This fishbone process is easily documented with fishbone diagrams as illustrated in diagrams the figure below. The influenced parameter is put on the center line and the influential factors are listed off of the centerline and can be grouped into major categories like Tool, Material, Work Methods and Environment.



Document The final step is to document all known information about the relationships relationships and sensitivities between the inputs and outputs. Some of the inputs may be correlated with each other as well as the outputs. and sensitivities There may be detailed mathematical models available from other studies or the information available may be vague such as for a machining process we know that as the feed rate increases, the quality of the finish decreases.

> It is best to document this kind of information in a table with all of the inputs and outputs listed both on the left column and on the top row. Then, correlation information can be filled in for each of the appropriate cells. See the case studies for an example.

Examples Click on each of the links below to see the process models for each of the case studies.

- 1. <u>Case Study 1 (Process Model)</u>
- 2. <u>Case Study 2 (Process Model)</u>

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3. Production Process Characterization

3.3. Data Collection for PPC

3.3.3. Define Sampling Plan

Sampling plan is detailed outline of measurements to be taken	A sampling plan is a detailed outline of which measurements will be taken at what times, on which material, in what manner, and by whom. Sampling plans should be designed in such a way that the resulting data will contain a representative sample of the parameters of interest and allow for all questions, as stated in the goals, to be answered.
Steps in the sampling plan	 The steps involved in developing a sampling plan are: 1. identify the parameters to be measured, the range of possible values, and the required resolution 2. design a sampling scheme that details how and when samples will be taken 3. select sample sizes 4. design data storage formats 5. assign roles and responsibilities
Verify and execute	Once the sampling plan has been developed, it can be verified and then passed on to the responsible parties for execution.



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3.3.3.1. Identifying Parameters, Ranges and Resolution



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3.3.3.1. Identifying Parameters, Ranges and Resolution

Our goals and the models we built in the previous steps should provide all of the information needed for selecting parameters and determining the expected ranges and the required measurement resolution.

Goals will tell us what to measure and how The first step is to carefully examine the goals. This will tell you which response variables need to be sampled and how. For instance, if our goal states that we want to determine if an oxide film can be grown on a wafer to within 10 Angstroms of the target value with a uniformity of <2%, then we know we have to measure the film thickness on the wafers to an accuracy of at least +/- 3 Angstroms and we must measure at multiple sites on the wafer in order to calculate uniformity.

The goals and the models we build will also indicate which explanatory variables need to be sampled and how. Since the fishbone diagrams define the known important relationships, these will be our best guide as to which explanatory variables are candidates for measurement.

Ranges helpDefining the expected ranges of values is useful for screening outliers.screen outliersIn the machining example, we would not expect to see many valuesthat vary more than +/- .005" from nominal. Therefore we know that
any values that are much beyond this interval are highly suspect and
should be remeasured.

Resolution helps choose measurement equipment	Finally, the required resolution for the measurements should be specified. This specification will help guide the choice of metrology equipment and help define the measurement procedures. As a rule of thumb, we would like our measurement resolution to be at least 1/10 of our tolerance. For the oxide growth example, this means that we want to measure with an accuracy of 2 Angstroms. Similarly, for the turning operation we would need to measure the diameter within .001". This means that vernier calipers would be adequate as the measurement device for this application.
Examples	Click on each of the links below to see the parameter descriptions for each of the case studies.
	1. <u>Case Study 1 (Sampling Plan)</u>
	2. <u>Case Study 2 (Sampling Plan)</u>





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- 3.3.3. Define Sampling Plan

3.3.3.2. Choosing a Sampling Scheme

A sampling scheme defines what data will be obtained and how	A sampling scheme is a detailed description of what data will be obtained and how this will be done. In PPC we are faced with two different situations for developing sampling schemes. The first is when we are conducting a controlled experiment. There are very efficient and exact methods for developing sampling schemes for designed experiments and the reader is referred to the <u>Process</u> <u>Improvement</u> chapter for details.
Passive data collection	The second situation is when we are conducting a passive data collection (PDC) study to learn about the inherent properties of a process. These types of studies are usually for comparison purposes when we wish to compare properties of processes against each other or against some hypothesis. This is the situation that we will focus on here.
There are two principles that guide our choice of sampling scheme	Once we have selected our response parameters, it would seem to be a rather straightforward exercise to take some measurements, calculate some statistics and draw conclusions. There are, however, many things which can go wrong along the way that can be avoided with careful planning and knowing what to watch for. There are two overriding principles that will guide the design of our sampling scheme.
The first is precision	The first principle is that of <i>precision</i> . If the sampling scheme is properly laid out, the difference between our estimate of some parameter of interest and its <i>true</i> value will be due only to random variation. The size of this random variation is measured by a quantity called <i>standard error</i> . The magnitude of the standard error is known as precision. The smaller the standard error, the more precise are our estimates.

Precision of an estimate depends on several factors The precision of any estimate will depend on:

- the inherent variability of the process estimator
- the measurement error
- the number of independent replications (sample size)
- the efficiency of the sampling scheme.

The second is systematic sampling error (or confounded effects) The second principle is the avoidance of systematic errors. Systematic sampling error occurs when the levels of one explanatory variable are the same as some other unaccounted for explanatory variable. This is also referred to as confounded effects. Systematic sampling error is best seen by example.

<u>Example 1:</u> We want to compare the effect of two different coolants on the resulting surface finish from a turning operation. It is decided to run one lot, change the coolant and then run another lot. With this sampling scheme, there is no way to distinguish the coolant effect from the lot effect or from tool wear considerations. There is systematic sampling error in this sampling scheme.

Example 2: We wish to examine the effect of two pre-clean procedures on the uniformity of an oxide growth process. We clean one cassette of wafers with one method and another cassette with the other method. We load one cassette in the front of the furnace tube and the other cassette in the middle. To complete the run, we fill the rest of the tube with other lots. With this sampling scheme, there is no way to distinguish between the effect of the different pre-clean methods and the cassette effect or the tube location effect. Again, we have systematic sampling errors.

Stratification helps to overcome systematic error The way to combat systematic sampling errors (and at the same time increase precision) is through stratification and randomization.
Stratification is the process of segmenting our population across levels of some factor so as to minimize variability within those segments or *strata*. For instance, if we want to try several different process recipes to see which one is best, we may want to be sure to apply each of the recipes to each of the three work shifts. This will ensure that we eliminate any systematic errors caused by a shift effect. This is where the ANOVA designs are particularly useful.

<i>Randomization</i> <i>helps too</i>	Randomization is the process of randomly applying the various treatment combinations. In the above example, we would not want to apply recipe 1, 2 and 3 in the same order for each of the three shifts but would instead randomize the order of the three recipes in each shift. This will avoid any systematic errors caused by the order of the recipes.
Examples	 The issues here are many and complicated. Click on each of the links below to see the sampling schemes for each of the case studies. 1. <u>Case Study 1 (Sampling Plan)</u> 2. <u>Case Study 2 (Sampling Plan)</u>

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- 3.3. Data Collection for PPC
- 3.3.3. Define Sampling Plan

3.3.3.3. Selecting Sample Sizes

Consider these things when selecting a sample size	 When choosing a sample size, we must consider the following issues: What population parameters we want to estimate Cost of sampling (importance of information) How much is already known Spread (variability) of the population Practicality: how hard is it to collect data How precise we want the final estimates to be
Cost of taking samples	The cost of sampling issue helps us determine how precise our estimates should be. As we will see below, when choosing sample sizes we need to select risk values. If the decisions we will make from the sampling activity are very valuable, then we will want low risk values and hence larger sample sizes.
Prior information	If our process has been studied before, we can use that prior information to reduce sample sizes. This can be done by using prior mean and variance estimates and by stratifying the population to reduce variation within groups.
Inherent variability	We take samples to form estimates of some characteristic of the population of interest. The variance of that estimate is proportional to the inherent variability of the population divided by the sample size:

 $\operatorname{Var}(\hat{\mathbf{p}}) \approx \sigma^2 / n$

with \hat{p} denoting the parameter we are trying to estimate. This means that if the variability of the population is large, then we must take many samples. Conversely, a small population variance means we don't have to take as many samples.

Practicality	Of course the sample size you select must make sense. This is where the trade-offs usually occur. We want to take enough observations to obtain reasonably precise estimates of the parameters of interest but we also want to do this within a practical resource budget. The important thing is to quantify the risks associated with the chosen sample size.
Sample size	In summary, the steps involved in estimating a sample size are:
determination	 There must be a statement about what is expected of the sample. We must determine what is it we are trying to estimate, how precise we want the estimate to be, and what are we going to do with the estimate once we have it. This should easily be derived from the goals.
	2. We must find some equation that connects the desired precision of the estimate with the sample size. This is a probability statement. A couple are given below; see your statistician if these are not appropriate for your situation.
	3. This equation may contain unknown properties of the population such as the mean or variance. This is where prior information can help.
	4. If you are stratifying the population in order to reduce variation, sample size determination must be performed for each stratum.
	5. The final sample size should be scrutinized for practicality. If it is unacceptable, the only way to reduce it is to accept less precision in the sample estimate.
Sampling proportions	When we are sampling proportions we start with a probability statement about the desired precision. This is given by:
	$Pr(\hat{p} - P \geq \delta) = \alpha$
	where
	 <i>p̂</i> is the estimated proportion P is the unknown population parameter
	• δ is the specified precision of the estimate
	• α is the probability value (usually low)

This equation simply shows that we want the probability that the precision of our estimate being less than we want is $\hat{\alpha}$. Of course we like to set $\hat{\alpha}$ low, usually .1 or less. Using some assumptions about the proportion being approximately normally distributed we can obtain an estimate of the required sample size as:
$$n=z_{lpha}^2(rac{pq}{\delta^2})$$

where z is the ordinate on the Normal curve corresponding to α .

Example Let's say we have a new process we want to try. We plan to run the new process and sample the output for yield (good/bad). Our current process has been yielding 65% (p=.65, q=.35). We decide that we want

the estimate of the new process yield to be accurate to within $\delta = .10$ at 95% confidence ($\Omega = .05$, z=2). Using the formula above we get a sample size estimate of *n*=91. Thus, if we draw 91 random parts from the output of the new process and estimate the yield, then we are 95%

EstimatingIf we are sampling continuous normally distributed variables, quitelocation:often we are concerned about the relative error of our estimates ratherrelative errorthan the absolute error. The probability statement connecting thedesired precision to the sample size is given by:

sure the yield estimate is within .10 of the true process yield.

$$Pr\left(\left\|rac{\hat{y}-\mu}{\mu}
ight\|\geq\delta
ight)=lpha$$

where μ is the (unknown) population mean and \overline{y} is the sample mean.

Again, using the normality assumptions we obtain the estimated sample size to be:

$$n pprox rac{z_lpha^2 \sigma^2}{\delta^2 \mu^2}$$

with σ^2 denoting the population variance.

If instead of relative error, we wish to use absolute error, the equation for sample size looks alot like the one for the case of proportions:

$$n pprox z_{lpha}^2 \left(rac{\sigma^2}{\delta^2}
ight)$$

where σ is the population standard deviation (but in practice is usually replaced by an *engineering guesstimate*).

Estimating location: absolute error *Example* Suppose we want to sample a stable process that deposits a 500 Angstrom film on a semiconductor wafer in order to determine the process mean so that we can set up a control chart on the process. We want to estimate the mean within 10 Angstroms ($\delta = 10$) of the true mean with 95% confidence ($\alpha = .05, Z = 2$). Our initial guess regarding the variation in the process is that one standard deviation is about 20 Angstroms. This gives a sample size estimate of n = 16. Thus, if we take at least 16 samples from this process and estimate the mean film thickness, we can be 95% sure that the estimate is within 10% of the true mean value.

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 Jata Collection for PPC

3.3.3. Define Sampling Plan

3.3.3.4. Data Storage and Retrieval

Data control depends on facility size If you are in a small manufacturing facility or a lab, you can simply design a sampling plan, run the material, take the measurements, fill in the run sheet and go back to your computer to analyze the results. There really is not much to be concerned with regarding data storage and retrieval.

In most larger facilities, however, the people handling the material usually have nothing to do with the design. Quite often the measurements are taken automatically and may not even be made in the same country where the material was produced. Your data go through a long chain of automatic acquisition, storage, reformatting, and retrieval before you are ever able to see it. All of these steps are fraught with peril and should be examined closely to ensure that valuable data are not lost or accidentally altered.

Know the process involved

- *now the* In the planning phase of the PPC, be sure to understand the entire data collection process. Things to watch out for include:
 - automatic measurement machines rejecting outliers
 - only summary statistics (mean and standard deviation) being saved
 - values for explanatory variables (location, operator, etc.) are not being saved
 - how missing values are handled

Consult withIt is important to consult with someone from the organizationsupport staffresponsible for maintaining the data system early in the planning phaseearly onof the PPC. It can also be worthwhile to perform some "dry runs" of the
data collection to ensure you will be able to actually acquire the data in
the format as defined in the plan.





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- 3.3.3. Define Sampling Plan

3.3.3.5. Assign Roles and Responsibilities

PPC is a teamIn today's manufacturing environment, it is unusual when an
investigative study is conducted by a single individual. Most PPC
studies will be a team effort. It is important that all individuals who
will be involved in the study become a part of the team from the
beginning. Many of the various collateral activities will need
approvals and sign-offs. Be sure to account for that cycle time in your
plan.

Table showing roles and potential responsibilities A partial list of these individuals along with their roles and potential responsibilities is given in the table below. There may be multiple occurrences of each of these individuals across shifts or process steps, so be sure to include everyone.

Tool Owner	Controls Tool	• Schedules tool time
	Operations	• Ensures tool state
		• Advises on
		experimental design
Process Owner	Controls Process	Advises on
	Recipe	experimental design
		• Controls recipe settings
Tool Operator	Executes	• Executes experimental
	Experimental Plan	runs
		• May take
		measurements
Metrology	Own Measurement	Maintains metrology
	Tools	equipment
		• Conducts gauge studies
		• May take
		measurements

CIM	Owns Enterprise	 Maintains data
	Information	collection system
	System	 Maintains equipment interfaces and data formatters
		• Maintains databases and information access
Statistician	Consultant	• Consults on experimental design
		 Consults on data analysis
Quality Control	Controls Material	• Ensures quality of incoming material
		 Must approve shipment of outgoing material (especially for recipe changes)

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3. Production Process Characterization

3.4. Data Analysis for PPC

In this section we will learn how to analyze and interpret the data we collected in accordance with our data collection plan.

Click on desired topic to read more	This section discusses the following topics:
	1. Initial Data Analysis
	1. Gather Data
	2. Quality Checking the Data
	3. Summary Analysis (Location, Spread and Shape)
	2. Exploring Relationships
	1. <u>Response Correlations</u>
	2. Exploring Main Effects
	3. Exploring First-Order Interactions
	3. Building Models
	1. Fitting Polynomial Models
	2. Fitting Physical Models
	4. Analyzing Variance Structure

- 5. <u>Assessing Process Stablility</u>
- 6. Assessing Process Capability
- 7. <u>Checking Assumptions</u>

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- 3. Production Process Characterization
- 3.4. Data Analysis for PPC

3.4.1. First Steps

Gather all After executing the data collection plan for the characterization study, the data must be gathered up for analysis. Depending on the scope of the of the data study, the data may reside in one place or in many different places. It into one may be in common factory databases, flat files on individual computers, place or handwritten on run sheets. Whatever the case, the first step will be to collect all of the data from the various sources and enter it into a single data file. The most convenient format for most data analyses is the variables-in-columns format. This format has the variable names in column headings and the values for the variables in the rows. Perform a The next step is to perform a quality check on the data. Here we are typically looking for data entry problems, unusual data values, missing quality data, etc. The two most useful tools for this step are the scatter plot and check on the data using the histogram. By constructing scatter plots of all of the response graphical variables, any data entry problems will be easily identified. Histograms and of response variables are also quite useful for identifying data entry numerical problems. Histograms of explanatory variables help identify problems techniques with the execution of the sampling plan. If the counts for each level of the explanatory variables are not the same as called for in the sampling plan, you know you may have an execution problem. Running numerical summary statistics on all of the variables (both response and explanatory) also helps to identify data problems. *Summarize* Once the data quality problems are identified and fixed, we should estimate the location, spread and shape for all of the response variables. data by This is easily done with a combination of histograms and numerical estimating summary statistics. location, spread and shape NIST



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3. Production Process Characterization

3.4. Data Analysis for PPC

3.4.2. Exploring Relationships

The first analysis of our data is exploration	Once we have a data file created in the desired format, checked the data integrity, and have estimated the summary statistics on the response variables, the next step is to start exploring the data and to try to understand the underlying structure. The most useful tools will be various forms of the basic scatter plot and box plot.
	These techniques will allow pairwise explorations for examining relationships between any pair of response variables, any pair of explanatory and response variables, or a response variable as a function of any two explanatory variables. Beyond three dimensions we are pretty much limited by our human frailties at visualization.
Graph everything that makes sense	In this exploratory phase, the key is to graph everything that makes sense to graph. These pictures will not only reveal any additional quality problems with the data but will also reveal influential data points and will guide the subsequent modeling activities.
Graph responses, then explanatory versus response, then conditional plots	The order that generally proves most effective for data analysis is to first graph all of the responses against each other in a pairwise fashion. Then we graph responses against the explanatory variables. This will give an indication of the main factors that have an effect on response variables. Finally, we graph response variables, conditioned on the levels of explanatory factors. This is what reveals interactions between explanatory variables. We will use nested <u>boxplots</u> and <u>block plots</u> to visualize interactions.

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3. Production Process Characterization

3.4. Data Analysis for PPC

3.4.2. Exploring Relationships

3.4.2.1. Response Correlations

Make scatter plots of all of the response variables	In this first phase of exploring our data, we plot all of the response variables in a pairwise fashion. The individual scatter plots are displayed in a matrix form with the y-axis scaling the same for all plots in a row of the matrix.
Check the slope of the data on the scatter plots	The <u>scatterplot matrix</u> shows how the response variables are related to each other. If there is a linear trend with a positive slope, this indicates that the responses are positively correlated. If there is a linear trend with a negative slope, then the variables are negatively correlated. If the data appear random with no slope, the variables are probably not correlated. This will be important information for subsequent model building steps.
This scatterplot matrix shows examples of both negatively and positively correlated variables	An example of a scatterplot matrix is given below. In this semiconductor manufacturing example, three responses, yield (Bin1), N-channel Id effective (NIDEFF), and P-channel Id effective (PIDEFF) are plotted against each other in a scatterplot matrix. We can see that Bin1 is positively correlated with NIDEFF and negatively correlated with PIDEFF. Also, as expected, NIDEFF is negatively correlated with PIDEFF. This kind of information will prove to be useful when we build models for yield improvement.





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3.4.2. Exploring Relationships

3.4.2.2. Exploring Main Effects

The next step is to look for main effects	The next step in the exploratory analysis of our data is to see which factors have an effect on which response variables and to quantify that effect. <u>Scatter plots</u> and <u>box plots</u> will be the tools of choice here.
Watch out for varying sample sizes across levels	This step is relatively self explanatory. However there are two points of caution. First, be cognizant of not only the trends in these graphs but also the amount of data represented in those trends. This is especially true for categorical explanatory variables. There may be many more observations in some levels of the categorical variable than in others. In any event, take unequal sample sizes into account when making inferences.
Graph implicit as well as explicit explanatory variables	The second point is to be sure to graph the responses against implicit explanatory variables (such as observation order) as well as the explicit explanatory variables. There may be interesting insights in these <i>hidden</i> explanatory variables.
Example: wafer processing	In the example below, we have collected data on the particles added to a wafer during a particular processing step. We ran a number of cassettes through the process and sampled wafers from certain slots in the cassette. We also kept track of which load lock the wafers passed through. This was done for two different process temperatures. We measured both small particles (< 2 microns) and large particles (> 2 microns). We plot the responses (particle counts) against each of the explanatory variables.
Cassette does not appear to be an important factor for small or large particles	This first graph is a <u>box plot</u> of the number of small particles added for each cassette type. The "X"'s in the plot represent the maximum, median, and minimum number of particles.

SMALL PARTICLES BY CASSETTE



The second graph is a box plot of the number of large particles added for each cassette type.

LARGE PARTICLES BY CASSETTE



We conclude from these two box plots that cassette does not appear to be an important factor for small or large particles.

We next generate box plots of small and large particles for the slot variable. First, the box plot forsmall particles.

There is a difference between slots for small particles, one slot is different for large particles



Next, the box plot for large particles.



We conclude that there is a difference between slots for small particles. We also conclude that one slot appears to be different for large particles.

We next generate box plots of small and large particles for the load lock variable. First, the box plot for small particles.

Load lock may have a slight effect for small and large particles SMALL PARTICLES BY LOAD LOCK



Next, the box plot for large particles.

LARGE PARTICLES BY LOAD LOCK



We conclude that there may be a slight effect for load lock for small and large particles.

For small We next generate box plots of small and large particles for the temperature variable. First, the box plot for small particles. particles, temperature has a strong effect on both location and spread. For large particles, there may be a slight temperature effect but this may just be due to the

to the outliers



Next, the box plot for large particles.



We conclude that temperature has a strong effect on both location and spread for small particles. We conclude that there might be a small temperature effect for large particles, but this may just be due to outliers.

1





<u>Production Process Characterization</u>
 <u>Data Analysis for PPC</u>

3.4.2. Exploring Relationships

3.4.2.3. Exploring First Order Interactions

It is important to identify interactions	The final step (and perhaps the most important one) in the exploration phase is to find any first order interactions. When the difference in the response between the levels of one factor is not the same for all of the levels of another factor we say we have an interaction between those two factors. When we are trying to optimize responses based on factor settings, interactions provide for compromise.
The eyes can be deceiving - be careful	Interactions can be seen visually by using nested <u>box plots</u> . However, caution should be exercised when identifying interactions through graphical means alone. Any graphically identified interactions should be verified by numerical methods as well.
Previous example continued	To continue the previous example, given below are nested box plots of the small and large particles. The load lock is nested within the two temperature values. There is some evidence of possible interaction between these two factors. The effect of load lock is stronger at the lower temperature than at the higher one. This effect is stronger for the smaller particles than for the larger ones. As this example illustrates, when you have significant interactions the main effects must be interpreted conditionally. That is, the main effects do not tell the whole story by themselves.
For small particles, the load lock effect is not as strong for high temperature as it is for low temperature	The following is the box plot of small particles for load lock nested within temperature.

SMALL PARTICLES



We conclude from this plot that for small particles, the load lock effect is not as strong for high temperature as it is for low temperature.

The same
may be true
for large
particles
but not as
stronglyThe following is the box plot of large particles for load lock nested within temperature.



We conclude from this plot that for large particles, the load lock effect may not be as strong for high temperature as it is for low temperature. However, this effect is not as strong as it is for small particles.

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- 3.4. Data Analysis for PPC

3.4.3. Building Models

Black box models When we develop a data collection plan we build *black box* models of the process we are studying like the one below:



3.4.3. Building Mo	dels
--------------------	------

Numerical models are explicit representations of our process model pictures	In the Exploring Relationships section, we looked at how to identify the input/output relationships through graphical methods. However, if we want to quantify the relationships and test them for statistical significance, we must resort to building mathematical models.
Polynomial models are generic descriptors of our output surface	There are two cases that we will cover for building mathematical models. If our goal is to develop an empirical prediction equation or to identify statistically significant explanatory variables and quantify their influence on output responses, we typically build <u>polynomial models</u> . As the name implies, these are polynomial functions (typically linear or quadratic functions) that describe the relationships between the explanatory variables and the response variable.
Physical models describe the underlying physics of our processes	On the other hand, if our goal is to fit an existing theoretical equation, then we want to build <u>physical models</u> . Again, as the name implies, this pertains to the case when we already have equations representing the physics involved in the process and we want to estimate specific parameter values.

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- 3. <u>Production Process Characterization</u> 3.4. Data Analysis for PPC
- 3.4.3. Building Models

3.4.3.1. Fitting Polynomial Models

Polynomial models are a great tool for determining which input factors drive responses and in what direction We use polynomial models to estimate and predict the shape of response values over a range of input parameter values. Polynomial models are a great tool for determining which input factors drive responses and in what direction. These are also the most common models used for analysis of designed experiments. A quadratic (second-order) polynomial model for two explanatory variables has the form of the equation below. The single x-terms are called the main effects. The squared terms are called the quadratic effects and are used to model curvature in the response surface. The cross-product terms are used to model interactions between the explanatory variables.

$$Y = \alpha_0 + \alpha_1 x_1 + \alpha_2 x_2 + \alpha_{11} x_1^2 + \alpha_{22} x_2^2 + \alpha_{12} x_1 x_2 + \varepsilon$$

We generally don't need more than second-order equations

Use multiple regression to fit polynomial models In most engineering and manufacturing applications we are concerned with at most second-order polynomial models. Polynomial equations obviously could become much more complicated as we increase the number of explanatory variables and hence the number of cross-product terms. Fortunately, we rarely see significant interaction terms above the two-factor level. This helps to keep the equations at a manageable level.

When the number of factors is small (less than 5), the complete polynomial equation can be fitted using the technique known as multiple regression. When the number of factors is large, we should use a technique known as *stepwise regression*. Most statistical analysis programs have a stepwise regression capability. We just enter all of the terms of the polynomial models and let the software choose which terms best describe the data. For a more thorough discussion of this topic and some examples, refer to the process improvement chapter.



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3. Production Process Characterization

3.4. Data Analysis for PPC

3.4.3. Building Models

3.4.3.2. Fitting Physical Models

Sometimes we want to use a physical model	Sometimes, rather than approximating response behavior with <u>polynomial</u> <u>models</u> , we know and can model the physics behind the underlying process. In these cases we would want to fit <i>physical models</i> to our data. This kind of modeling allows for better prediction and is less subject to variation than polynomial models (as long as the underlying process doesn't change).
We will use a CMP process to illustrate	We will illustrate this concept with an example. We have collected data on a chemical/mechanical planarization process (CMP) at a particular semiconductor processing step. In this process, wafers are polished using a combination of chemicals in a polishing slurry using polishing pads. We polished a number of wafers for differing periods of time in order to calculate material removal rates.
CMP removal rate can be modeled with a non-linear equation	From first principles we know that removal rate changes with time. Early on, removal rate is high and as the wafer becomes more planar the removal rate declines. This is easily modeled with an exponential function of the form: $removal rate = p1 + p2 \ge p3 \ge time$ where $p1$, $p2$, and $p3$ are the parameters we want to estimate.
A non-linear	The equation was fit to the data using a non-linear regression routine. A plot of the original data and the fitted line are given in the image below. The fit is quite

good. This fitted equation was subsequently used in process optimization work.

non-linear regression routine was used to fit the data to the equation



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3. Production Process Characterization

3.4. Data Analysis for PPC

3.4.4. Analyzing Variance Structure

Studying variation is important in PPC	One of the most common activities in process characterization work is to study the variation associated with the process and to try to determine the important sources of that variation. This is called <i>analysis of variance</i> . Refer to the section of this chapter on <u>ANOVA models</u> for a discussion of the theory behind this kind of analysis.
The key is to know the structure	The key to performing an analysis of variance is identifying the <i>structure</i> represented by the data. In the ANOVA models section we discussed <u>one-way</u> layouts and two-way layouts where the factors are either <u>crossed</u> or <u>nested</u> . Review these sections if you want to learn more about ANOVA structural layouts.
	To perform the analysis, we just identify the structure, enter the data for each of the factors and levels into a statistical analysis program and then interpret the ANOVA table and other output. This is all illustrated in the example below.
Example: furnace oxide thickness with a 1-way layout	The example is a furnace operation in semiconductor manufacture where we are growing an oxide layer on a wafer. Each lot of wafers is placed on quartz containers (boats) and then placed in a long tube-furnace. They are then raised to a certain temperature and held for a period of time in a gas flow. We want to understand the important factors in this operation. The furnace is broken down into four sections (zones) and two wafers from each lot in each zone are measured for the thickness of the oxide layer.
Look at effect of zone location on oxide thickness	The first thing to look at is the effect of zone location on the oxide thickness. This is a classic one-way layout. The factor is furnace zone and we have four levels. A plot of the data and an ANOVA table are given below.

The zone effect is masked by the lot-to-lot variation



ANOVA Analysis of Variance

table

Source	DF	<u>SS</u>	Mean Square	<u>F Ratio</u>	$\underline{\text{Prob}} > \underline{\text{F}}$
Zone	3	912.6905	304.23	0.467612	0.70527
Within	164	106699.1	650.604		

From the graph there does not appear to be much of a zone effect; in fact, the ANOVA table Let's indicates that it is not significant. The problem is that variation due to lots is so large that it is account for lot with a masking the zone effect. We can fix this by adding a factor for lot. By treating this as a nested nested two-way layout, we obtain the ANOVA table below. layout

Now both	Analysis of Variance
lot and zone	

are revealed as Source DF SS Mean Square F Ratio Prob > Fimportant 61442.29 3072.11 5.37404 1.39e-7 Lot 20 4.72864 3.9e-11 Zone[lot] 63 36014.5 571.659 Within 10155 120.893 84

Since the "Prob > F" is less than .05, for both lot and zone, we know that these factors are **Conclusions** statistically significant at the 95% level of confidence.

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3.4.5. Assessing Process Stability

A process is stable if it has a constant mean and a constant variance over time A manufacturing process cannot be released to production until it has been proven to be stable. Also, we cannot begin to talk about <u>process</u> <u>capability</u> until we have demonstrated stability in our process. A process is said to be stable when all of the response parameters that we use to measure the process have both constant means and constant variances over time, and also have a constant distribution. This is equivalent to our earlier definition of <u>controlled variation</u>.

The graphical tool we use to assess stability is the scatter plot or the control chart

The graphical tool we use to assess process stability is the <u>scatter</u> <u>plot</u>. We collect a sufficient number of independent samples (greater than 100) from our process over a sufficiently long period of time (this can be specified in days, hours of processing time or number of parts processed) and plot them on a scatter plot with sample order on the x-axis and the sample value on the y-axis. The plot should look like constant random variation about a constant mean. Sometimes it is helpful to calculate <u>control limits</u> and plot them on the scatter plot along with the data. The two plots in the <u>controlled variation</u> example are good illustrations of stable and unstable processes.

Numerically, we assess its stationarity using the autocorrelation function

Graphical methods usually good enough Numerically, we evaluate process stability through a times series analysis concept know as <u>stationarity</u>. This is just another way of saying that the process has a constant mean and a constant variance. The numerical technique used to assess stationarity is the <u>autocovariance function</u>.

Typically, graphical methods are good enough for evaluating process stability. The numerical methods are generally only used for modeling purposes.





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3. Production Process Characterization

3.4. Data Analysis for PPC

3.4.6. Assessing Process Capability

Capability compares a process against its specification

Process capability analysis entails comparing the performance of a process against its specifications. We say that a process is capable if virtually all of the possible variable values fall within the specification limits.

Use a capability chart Graphically, we assess process capability by plotting the process specification limits on a histogram of the observations. If the histogram falls within the specification limits, then the process is capable. This is illustrated in the graph below. Note how the process is shifted below target and the process variation is too large. This is an example of an incapable process.

Notice how the process is off target and has too much variation



Numerically, we measure capability with a capability index. The general equation for the capability index, C_p , is:

Numerically, we use the C_p index

$$Cp = \frac{USL - LSL}{6s}$$

InterpretationThis equation just says that the measure of our process capability is how much of our observed
process variation is covered by the process specifications. In this case the process variation is
measured by 6 standard deviations (+/- 3 on each side of the mean). Clearly, if $C_p > 1.0$, then the
process specification covers almost all of our process observations.

 C_p does notThe only problem with with the C_p index is that it does not account for a process that is off-center.account forWe can modify this equation slightly to account for off-center processes to obtain the C_{pk} index asprocess thatfollows:

Or the
$$C_{pk}$$

index $Cpk = \min\left[\frac{USL - \overline{x}}{3s}, \frac{\overline{x} - LSL}{3s}\right]$

 C_{pk} accountsThis equation just says to take the minimum distance between our specification limits and the
process mean and divide it by 3 standard deviations to arrive at the measure of process capability.
This is all covered in more detail in the process capability section of the process monitoring chapter.
For the example above, note how the C_{pk} value is less than the C_p value. This is because the process
distribution is not centered between the specification limits.

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3. Production Process Characterization

3.4. Data Analysis for PPC

3.4.7. Checking Assumptions

Check the Many of the techniques discussed in this chapter, such as hypothesis tests, control charts and capability indices, assume that the underlying structure of the data can be adequately modeled by a normality of normal distribution. Many times we encounter data where this is not the case.

Some causes of nonnormality

the data

There are several things that could cause the data to appear non-normal, such as:

- The data come from two or more different sources. This type of data will often have a multi-modal distribution. This can be solved by identifying the reason for the multiple sets of data and analyzing the data separately.
- The data come from an unstable process. This type of data is nearly impossible to analyze because the results of the analysis will have no credibility due to the changing nature of the process.
- The data were generated by a stable, yet fundamentally non-normal mechanism. For example, particle counts are non-normal by the very nature of the particle generation process. Data of this type can be handled using transformations.

We can sometimes transform the data to make it look normal

For the last case, we could try transforming the data using what is known as a *power transformation*. The power transformation is given by the equation:

$$Y^{\left(\lambda\right)} = \begin{cases} y^{\lambda} & \text{if } \lambda \neq 0\\ \ln(y) & \text{if } \lambda = 0 \end{cases}$$

where Y represents the data and lambda is the transformation value. Lambda is typically any value between -2 and 2. Some of the more common values for lambda are 0, 1/2, and -1, which give the following transformations:

$$\ln(y), \sqrt{y}, \frac{1}{y}$$

General algorithm for trying to make non-normal data approximately normal

The general algorithm for trying to make non-normal data appear to be approximately normal is to: 1. Determine if the data are non-normal. (Use normal probability plot and histogram).

2. Find a transformation that makes the data look approximately normal, if possible. Some data sets may include zeros (i.e., particle data). If the data set does include zeros, you must first add a constant value to the data and then transform the results.
Example: particle count data As an example, let's look at some particle count data from a semiconductor processing step. Count data are inherently non-normal. Below are histograms and normal probability plots for the original data and the ln, sqrt and inverse of the data. You can see that the log transform does the best job of making the data appear as if it is normal. All analyses can be performed on the log-transformed data and the assumptions will be approximately satisfied.



Neither the square root nor the inverse transformation looks normal





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3. Production Process Characterization

3.5. Case Studies

Summary This section presents several case studies that demonstrate the application of production process characterizations to specific problems.

Table of The following case studies are available. Contents

- 1. Furnace Case Study
 - 2. Machine Case Study





- 3. Production Process Characterization
- 3.5. Case Studies

3.5.1. Furnace Case Study

Introduction	This case study analyzes a furnace oxide growth process.
Table of Contents	 The case study is broken down into the following steps. 1. <u>Background and Data</u> 2. <u>Initial Analysis of Response Variable</u> 3. <u>Identify Sources of Variation</u> 4. <u>Analysis of Variance</u> 5. <u>Final Conclusions</u> 6. <u>Work This Example Yourself</u>





3. Production Process Characterization

3.5. <u>Case Studies</u>

3.5.1. Furnace Case Study

3.5.1.1. Background and Data

Introduction	In a semiconductor manufacturing process flow, we have a step whereby we grow an oxide film on the silicon wafer using a furnace. In this step, a cassette of wafers is placed in a quartz "boat" and the boats are placed in the furnace. The furnace can hold four boats. A gas flow is created in the furnace and it is brought up to temperature and held there for a specified period of time (which corresponds to the desired oxide thickness). This study was conducted to determine if the process was stable and to characterize sources of variation so that a process control strategy could be developed.
Goal	The goal of this study is to determine if this process is capable of consistently growing oxide films with a thickness of 560 Angstroms +/- 100 Angstroms. An additional goal is to determine important sources of variation for use in the development of a process control strategy.
Process Model	In the picture below we are modeling this process with one output (film thickness) that is influenced by four controlled factors (gas flow, pressure, temperature and time) and two uncontrolled factors (run and zone). The four controlled factors are part of our recipe and will remain constant throughout this study. We know that there is run-to-run variation that is due to many different factors (input material variation, variation in consumables, etc.). We also know that the different zones in the furnace have an effect. A zone is a region of the furnace tube that holds one boat. There are four zones in these

tubes. The zones in the middle of the tube grow oxide a little bit differently from the ones on the ends. In fact, there are temperature

offsets in the recipe to help minimize this problem.



Sensitivity Model The sensitivity model for this process is fairly straightforward and is given in the figure below. The effects of the machin are mostly related to the preventative maintenance (PM) cycle. We want to make sure the quartz tube has been cleaned recently, the mass flow controllers are in good shape and the temperature controller has been calibrated recently. The same is true of the measurement equipment where the thickness readings will be taken. We want to make sure a <u>gauge study</u> has been performed. For material, the incoming wafers will certainly have an effect on the outgoing thickness as well as the quality of the gases used. Finally, the recipe will have an effect including gas flow, temperature offset for the different zones, and temperature profile (how quickly we raise the temperature, how long we hold it and how quickly we cool it off).



SamplingGiven our goal statement and process modeling, we can now define a
sampling plan. The primary goal is to determine if the process is
capable. This just means that we need to monitor the process over some
period of time and compare the estimates of process location and spread
to the specifications. An additional goal is to identify sources of
variation to aid in setting up a process control strategy. Some obvious
sources of variation are incoming wafers, run-to-run variability,
variation due to operators or shift, and variation due to zones within a
furnace tube. One additional constraint that we must work under is that
this study should not have a significant impact on normal production
operations.

Given these constraints, the following sampling plan was selected. It was decided to monitor the process for one day (three shifts). Because this process is operator independent, we will not keep shift or operator information but just record run number. For each run, we will randomly assign cassettes of wafers to a zone. We will select two wafers from each zone after processing and measure two sites on each wafer. This plan should give reasonable estimates of run-to-run variation and within zone variability as well as good overall estimates of process location and spread.

We are expecting readings around 560 Angstroms. We would not expect many readings above 700 or below 400. The measurement equipment is accurate to within 0.5 Angstroms which is well within the accuracy needed for this study.

Data

The following are the data that were collected for this study.

RUN	ZONE	WAFER	THICKNESS
1	1	1	546
1	1	2	540
1	2 2	1	566
1		2	564
1	3	1	577
1	3	2	546
1	4	1	543
1	4	2	529
2	1	1	561
2	1	2	556
2	2 2	1	577
2 2	2	2	553
2	3	1	563
2	3	2	577
2	4	1	556
2	4	2	540
3	1	1	515
3	1	2	520
3 3 3 3	2	1	548
3	2	2	542
	3	1	505
3 3	3	2	487
3	4	1	506
3 4	4	2	514
4 4	1	1	568
	1	2	584
4 4	2	1 2	570 545
4 4	2 3	1	589
4	3	2	562
4	4	1	569
4	4		571
5		2 1	550
5	1 1 2 2 3 3	2	550
5	2	1	562
5 5 5 5 5 5 5 5 5 5	2	1 2 1	580
5	3	1	560
5	3		554
5	4	2 1	545
5	4	2	546
6	1	2 1	584
6 6	1	2	581
6	2	1	567
6 6	2	2	558
6	4 1 1 2 2 3 3	2 1 2 1 2	556
б	3	2	560
6	4	1	591
б	4	2	599

3.5.1.1. Background and Data

-	1	1	F 0 2
7	1	1	593
7	1	2	626
7	2	1	584
7 7 7	2 2 3 3	2 1	559
7	3	1	634
7		2	598
7	4	1	569
7	4	2	592
8	1	1	522
8	1 1	2	535
8	2	1	535
8	2	2	581
8	2 2 3 3	2 1 2 1 2 1 2 1 2	527
8	3	2	520
8	4	1	532
8	4	2	539
9	1	1 2 1	562
9	4 1 1	2	568
9	2	1	548
9	2	2	548
9	2	1	533
9	2 2 3 3	2 1 2	553
9	4	1	533
9	4	2	521
10	1	1	555
10	1 1	1 2	545
10		1	584
10	2	2	572
10	2 2 3	1	546
10	3	1 2 1	552
10	3 4 4	1	586
10	4	2	584
11	1	1	565
11			557
	1	2 1	583
11 11	2 2 3	2	585
11	2	∠ 1	
	3	1 2	582 567
11	3 4		
11		1 2	549
11	4	1	533
12	1	1 2	548
12	1	2	528
12	2	1	563
12	2 2 3	2	588
12	3	1 2	543
12	3 4	2	540
12		1	585
12	4	2	586
13	1	1	580
13	1	2 1	570
13	1 2 2 3		556
13	2	2	569
13	3	1	609
13	3	2	625

3.5.1.1. Background and Data

13	4	1	570
13	4	2	595
14	1	1	564
14	1	2	555
14	2	1	585
14	2	2	588
	2		
14	3	1	564
14	3	2	583
14	4	1	563
14	4	2	558
15	1	1	550
15	1	2	557
15	2	1	538
15	2	2	525
15	3	1	556
15	3	2	547
15	4	1	534
15	4	2	542
16	1	1	552
16	1	2	547
	2	1	563
16			
16	2	2	578
16	3	1	571
16	3	2	572
16	4	1	575
16	4	2	584
17	1	1	549
17	1	2	546
	2	1	584
17			
17	2	2	593
17	3	1	567
17	3	2	548
	4	1	606
17			
17	4	2	607
18	1	1	539
18	1	2	554
18	2	1	533
18	2	2	535
18	3	1	522
18	3	2	521
18	4	1	547
18	4	2	550
19	1	1	610
19	1	2	592
19	2	1	587
19	2	2	587
19	3	1	572
19	3	2	612
19	4	1	566
19	4	2	563
20	1	1	569
20	1	2	609
20	2	1	558
	2	2	
20	2	2	555

3.5.1.1. Background and Data

20	3	1	577
20	3	2	579
20	4	1	552
20	4	2	558
21	1	1	595
21	1	2	583
21	2	1	599
21	2	2	602
21	3	1	598
21	3	2	616
21	4	1	580
21	4	2	575

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- 3. Production Process Characterization
- 3.5. Case Studies
- 3.5.1. Furnace Case Study

3.5.1.2. Initial Analysis of Response Variable

Initial Plots of Response Variable The initial step is to assess data quality and to look for anomalies. This is done by generating a <u>normal probability plot</u>, a <u>histogram</u>, and a <u>boxplot</u>. For convenience, these are generated on a single page.



Conclusions From the Plots We can make the following conclusions based on these initial plots.

- The box plot indicates one outlier. However, this outlier is only slightly smaller than the other numbers.
- The normal probability plot and the histogram (with an overlaid normal density) indicate that this data set is reasonably approximated by a normal distribution.

3.5.1.2. Initial Analysis of Response Variable

ParameterParameter estimates for the film thickness are summarized in the
following table.

Туре	Parameter	Estimate	Lower (95%) Confidence Bound	Upper (95%) Confidence Bound
Location	Mean	563.0357	559.1692	566.9023
Dispersion	Standard Deviation	25.3847	22.9297	28.4331

Parameter Estimates

Quantiles Quantiles for the film thickness are summarized in the following table.

Quantu	Quantiles for Film Thickness					
100.0%	Maximum	634.00				
99.5%		634.00				
97.5%		615.10				
90.0%		595.00				
75.0%	Upper Quartile	582.75				
50.0%	Median	562.50				
25.0%	Lower Quartile	546.25				
10.0%		532.90				
2.5%		514.23				
0.5%		487.00				
0.0%	Minimum	487.00				

Quantiles for Film Thickness

CapabilityFrom the above preliminary analysis, it looks reasonable to proceed with the capability
analysis.Analysisanalysis.



Dataplot generated the following capability analysis.



3.5.1.2. Initial Analysis of Response Variable

*	UPPER SPEC LIMIT (USL)	=		*
*	TARGET (TARGET)	=	560.00000	*
*	USL COST (USLCOST)	=	UNDEFINED	*
* * :	* * * * * * * * * * * * * * * * * * * *	* * * * *	* * * * * * * * * * *	* *
*	CP	=	1.31313	*
*	CP LOWER 95% CI	=	1.17234	*
*	CP UPPER 95% CI	=	1.45372	*
*	CPL	=	1.35299	*
*	CPL LOWER 95% CI	=	1.21845	*
*	CPL UPPER 95% CI	=	1.48753	*
*	CPU	=	1.27327	*
*	CPU LOWER 95% CI	=	1.14217	*
*	CPU UPPER 95% CI	=	1.40436	*
*	СРК	=	1.27327	*
*	CPK LOWER 95% CI	=	1.12771	*
*	CPK UPPER 95% CI	=	1.41882	*
*	CNPK	=	1.35762	*
*	СРМ	=	1.30384	*
*	CPM LOWER 95% CI	=	1.16405	*
*	CPM UPPER 95% CI	=	1.44344	*
*	CC	=	0.00460	*
*	ACTUAL % DEFECTIVE	=	0.00000	*
*	THEORETICAL % DEFECTIVE	=	0.00915	*
*	ACTUAL (BELOW) % DEFECTIVE	=	0.00000	*
*	THEORETICAL (BELOW) % DEFECTIVE	=	0.00247	*
*	ACTUAL (ABOVE) % DEFECTIVE	=	0.00000	*
*	THEORETICAL (ABOVE) % DEFECTIVE	=	0.00668	*
*	EXPECTED LOSS	=	UNDEFINED	*
* * *	***************************************	* * * * *	-	* *

Summary of Percent Defective

bf From the above capability analysis output, we can summarize the percent defective (i.e., the number of items outside the specification limits) in the following table.

Specification	Value	Percent	Actual	Theoretical (% Based On Normal)
Lower Specification Limit	460	Percent Below LSL = $100*\Phi$ ((LSL - \overline{y})/s)	0.0000	0.0025%
Upper Specification Limit	660	Percent Above USL = $100*(1 - \mathbf{\Phi})$ ((USL - $\overline{\mathbf{y}}$)/s))	0.0000	0.0067%
Specification Target	560	Combined Percent Below LSL and Above USL	0.0000	0.0091%
Standard Deviation	25.38468			

Percentage Outside Specification Limits

with Φ denoting the normal cumulative distribution function, \overline{y} the sample mean, and s the sample standard deviation.

Summary of
CapabilityFrom the above capability analysis output, we can summarize various capability index
statistics in the following table.Index
StatisticsCapability Index StatisticsCapability Statistic Index Lower CI Upper CI

Capability Statistic	Index	Lower CI	Upper CI
СР	1.313	1.172	1.454
СРК	1.273	1.128	1.419
СРМ	1.304	1.165	1.442
CPL	1.353	1.218	1.488
CPU	1.273	1.142	1.404

Conclusions The above capability analysis indicates that the process is capable and we can proceed with the analysis.

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- 3. Production Process Characterization
- 3.5. Case Studies
- 3.5.1. Furnace Case Study

3.5.1.3. Identify Sources of Variation

The next part of the analysis is to break down the sources of variation.

Box Plot by The following is a <u>box plot</u> of the thickness by run number. Run



Conclusions From Box Plot We can make the following conclusions from this box plot.

- 1. There is significant run-to-run variation.
- 2. Although the means of the runs are different, there is no discernable trend due to run.
- 3. In addition to the run-to-run variation, there is significant within-run variation as well. This suggests that a box plot by furnace location may be useful as well.





Conclusions From Box Plot	 We can make the following conclusions from this box plot. 1. There is considerable variation within a given furnace location. 2. The variation between furnace locations is small. That is, the locations and scales of each of the four furnace locations are fairly comparable (although furnace location 3 seems to have a few mild outliers).
	have a few finite outliers).

Box Plot by The following is a <u>box plot</u> of the thickness by wafer. *Wafer*



Conclusion From this box plot, we conclude that wafer does not seem to be a significant factor. *From Box*

Plot

Block Plot In order to show the combined effects of run, furnace location, and wafer, we draw a <u>block plot</u> of the thickness. Note that for aesthetic reasons, we have used connecting lines rather than enclosing boxes.



Conclusions From Block Plot	We can draw the following conclusions from this block plot.1. There is significant variation both between runs and between furnace locations. The between-run variation appears to be greater.
	2 Pup 2 sooms to be an outlier

2. Run 3 seems to be an outlier.





- 3. Production Process Characterization
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3.5.1.4. Analysis of Variance

Analysis of Variance The next step is to confirm our interpretation of the plots in the previous section by running an analysis of variance.

In this case, we want to run a nested analysis of variance. Although Dataplot does not perform a nested analysis of variance directly, in this case we can use the Dataplot ANOVA command with some additional computations to generate the needed analysis.

The basic steps are to use a one-way ANOA to compute the appropriate values for the run variable. We then run a one-way ANOVA with all the combinations of run and furnace location to compute the "within" values. The values for furnace location nested within run are then computed as the difference between the previous two ANOVA runs.

The <u>Dataplot macro</u> provides the details of this computation. This computation can be summarized in the following table.

Source	Degrees of Freedom	Sum of Squares	Mean Square Error	F Ratio	Prob > F
Run	20	61,442.29	3,072.11	5.37404	0.0000001
Furnace Location [Run]	63	36,014.5	571.659	4.72864	3.85e-11
Within	84	10,155	120.893		
Total	167	107,611.8	644.382		

Analysis of Variance

Components of Variance

From the above analysis of variance table, we can compute the components of variance. Recall that for this data set we have 2 wafers measured at 4 furnace locations for 21 runs. This leads to the following set of equations.

3072.11 = (4*2)*Var(Run) + 2*Var(Furnace Location) + Var(Within) 571.659 = 2*Var(Furnace Location) + Var(Within) 120.893 = Var(Within)

Solving these equations yields the following components of variance table.

Component	Variance Component	Percent of Total	Sqrt(Variance Component)
Run	312.55694	47.44	17.679
Furnace Location[Run]	225.38294	34.21	15.013
Within	120.89286	18.35	10.995

Components of Variance



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3. Production Process Characterization

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- 3.5.1. Furnace Case Study

3.5.1.5. Final Conclusions

Final Conclusions

This simple study of a furnace oxide growth process indicated that the process is capable and showed that both run-to-run and zone-within-run are significant sources of variation. We should take this into account when designing the control strategy for this process. The results also pointed to where we should look when we perform process improvement activities.





- 3. Production Process Characterization
- 3.5. Case Studies
- 3.5.1. Furnace Case Study

3.5.1.6. Work This Example Yourself

<u>View</u>
<u>Dataplot</u>
<u>Macro for</u>
this Case
<u>Study</u>

This page allows you to repeat the analysis outlined in the case study description on the previous page using <u>Dataplot</u>, if you have <u>downloaded and installed it</u>. Output from each analysis step below will be displayed in one or more of the Dataplot windows. The four main windows are the Output window, the Graphics window, the Command History window and the Data Sheet window. Across the top of the main windows there are menus for executing Dataplot commands. Across the bottom is a command entry window where commands can be typed in.

Data Analysis Steps	Results and Conclusions
Click on the links below to start Dataplot and run this case study yourself. Each step may use results from previous steps, so please be patient. Wait until the software verifies that the current step is complete before clicking on the next step.	The links in this column will connect you with more detailed information about each analysis step from the case study description.
1. Get set up and started.	
<u>1. Read in the data.</u>	<u>1. You have read 4 columns of numbers</u> <u>into Dataplot, variables run, zone,</u> wafer, and filmthic.

1. Initial plots indicate that the film thickness is reasonably approximated by a normal distribution with no significant outliers.
2. Mean is 563.04 and standard deviation is 25.38. Data range from 487 to 634.
3. Capability analysis indicates that the process is capable.
1. The box plot shows significant variation both between runs and within runs.
2. The box plot shows significant variation within furnace location but not between furnace location.
<u>3. The box plot shows no significant</u> <u>effect for wafer.</u>
<u>4. The block plot shows both run</u> <u>and furnace location are</u> <u>significant.</u>

In

4. Perform an Analysis of Variance 1. Perform the analysis of variance and compute the components of variance.	1. The results of the ANOVA are summarized in an ANOVA table and a components of variance table.
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- 3. Production Process Characterization
- 3.5. Case Studies

3.5.2. Machine Screw Case Study

Introduction This case study analyzes three automatic screw machines with the intent of replacing one of them.

Table of The case study is broken down into the following steps.

- Contents
- 1. Background and Data
- 2. <u>Box Plots by Factor</u>
- 3. Analysis of Variance
- 4. <u>Throughput</u>
- 5. Final Conclusions
- 6. Work This Example Yourself

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- 3. Production Process Characterization
- 3.5. Case Studies
- 3.5.2. Machine Screw Case Study

3.5.2.1. Background and Data

Introduction	A machine shop has three automatic screw machines that produce various parts. The shop has enough capital to replace one of the machines. The quality control department has been asked to conduct a study and make a recommendation as to which machine should be replaced. It was decided to monitor one of the most commonly produced parts (an 1/8 th inch diameter pin) on each of the machines and see which machine is the least stable.
Goal	The goal of this study is to determine which machine is least stable in manufacturing a steel pin with a diameter of .125 +/003 inches. Stability will be measured in terms of a constant variance about a constant mean. If all machines are stable, the decision will be based on process variability and throughput. Namely, the machine with the highest variability and lowest throughput will be selected for replacement.
Process Model	The process model for this operation is trivial and need not be addressed.
Sensitivity Model	The sensitivity model, however, is important and is given in the figure below. The material is not very important. All machines will receive barstock from the same source and the coolant will be the same. The method is important. Each machine is slightly different and the operator must make adjustments to the speed (how fast the part rotates), feed (how quickly the cut is made) and stops (where cuts are finished) for each machine. The same operator will be running all three machines simultaneously. Measurement is not too important. An experienced QC engineer will be collecting the samples and making the measurements. Finally, the machine condition is really what this study is all about. The wear on the ways and the lead screws will largely determine the stability of the machining process. Also, tool wear is important. The tool insert wear will be monitored by the operator

and they will be changed as needed.



Sampling Given our goal statement and process modeling, we can now define a sampling plan. The primary goal is to determine if the process is stable and to compare the variances of the three machines. We also need to monitor throughput so that we can compare the productivity of the three machines.

There is an upcoming three-day run of the particular part of interest, so this study will be conducted on that run. There is a suspected time-of-day effect that we must account for. It is sometimes the case that the machines do not perform as well in the morning, when they are first started up, as they do later in the day. To account for this we will sample parts in the morning and in the afternoon. So as not to impact other QC operations too severely, it was decided to sample 10 parts, twice a day, for three days from each of the three machines. Daily throughput will be recorded as well.

We are expecting readings around $.125 \pm .003$ inches. The parts will be measured using a standard micrometer with readings recorded to 0.0001 of an inch. Throughput will be measured by reading the part counters on the machines at the end of each day.

3.5.2.1. Background and Data

Data The following are the data that were collected for this study.

MACHINE (1-3)	DAY (1-3)	TIME 1 = AM 2 = PM	SAMPLE (1-10)	DIAMETER (inches)
	(1-3)		(1-10) 1 2 3 4 5 6 7 8 9 10 10 1 2 3 4 5 6 7 8 9 10	0.1247 0.1264 0.1252 0.1253 0.1253 0.1263 0.1251 0.1254 0.1235 0.1257 0.1257 0.1257 0.1257 0.1257 0.1253 0.1265 0.1254 0.1244 0.1244 0.1244 0.1241 0.1251 0.1251 0.1255 0.1255 0.1255 0.1255 0.1255 0.1266 0.1244 0.1243 0.1248
1 1 1 1 1 1 1	2 2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2 2	1 2 3 4 5 6 7 8	0.1248 0.1235 0.1243 0.1265 0.127 0.1229 0.125 0.1248

Data				
1	2	2	9	0.1252
1	2	2	10	0.1243
1	3	1	1	0.1255
1	3	1	2	0.1237
1	3	1	3	0.1235
1	3	1	4	0.1264
	3			
1		1	5	0.1239
1	3	1	6	0.1266
1	3	1	7	0.1242
1	3	1	8	0.1231
1	3	1	9	0.1232
1	3	1	10	0.1244
1	3	2	1	0.1233
1	3	2	2	0.1237
1	3	2	3	0.1244
1	3	2	4	0.1254
1	3	2	5	0.1247
1	3	2	6	0.1254
1	3	2	7	0.1258
1	3	2	8	0.126
1	3	2	9	0.1235
1	3	2	10	0.1273
2	1	1	1	0.1239
2	1	1	2	0.1239
2	1	1	3	0.1239
2	1	1	4	0.1231
2	1	1	5	0.1221
2	1	1	6	0.1216
2	1	1	7	0.1233
2	1	1	8	0.1228
2	1	1	9	0.1227
2	1	1	10	0.1229
2	1	2	1	0.122
2	1	2	2	0.1239
2	1	2	3	0.1237
2	1	2	4	0.1216
2	1	2	5	0.1235
2	1	2	6	0.124
2	1	2	7	0.1224
2	1	2	8	0.1236
2	1	2	9	0.1236
2	1	2	10	0.1217
2	2	1	1	0.1247
2	2	1	2	0.122
2	2	1	3	0.1218
2	2	1	4	0.1237
4	2	Ŧ	Т	0.145/

nu Dala				
2	2	1	5	0.1234
2	2	1	6	0.1229
2	2	1	7	0.1235
2	2	1	8	0.1237
2	2	1	9	0.1224
2	2	1	10	0.1224
2	2	2	1	0.1239
2	2	2	2	0.1226
2	2	2	3	0.1224
2	2	2	4	0.1239
2	2	2	5	0.1237
2	2	2	6	0.1227
2	2	2	7	0.1218
2	2	2	8	0.122
2	2	2	9	0.1231
2	2	2	10	0.1244
2	3	1	1	0.1219
2	3	1	2	0.1243
2	3	1	3	0.1243
2	3	1	4	0.1223
2	3	1	5	0.1223
2	3	1	6	0.1218
2	3	1	7	0.1225
2	3	1	8	0.1238
2	3	1	9	0.1244
2	3	1	10	0.1236
2	3	2	1	0.1231
2	3	2	2	0.1223
2	3	2	3	0.1241
2	3	2	4	0.1215
2	3	2	5	0.1221
2	3	2	6	0.1236
2	3	2	7	0.1229
2	3	2	8	0.1205
2	3	2	9	0.1241
2	3	2	10	0.1232
3	1	1	1	0.1255
3	1	1	2	0.1215
3	1	1	3	0.1219
3	1	1	4	0.1253
3 3 3 3 3 3 3 3 3 3 3	1	1	5	0.1232
3	1	1	б	0.1266
3	1	1	7	0.1271
3	1	1	8	0.1209
3	1	1	9	0.1212
3	1	1	10	0.1249

С	1	2	1	0 1 2 2 0
3	1	2		0.1228
3	1	2	2	0.126
3	1	2	3	0.1242
2				
3	1	2	4	0.1236
3	1	2	5	0.1248
3	1	2	6	0.1243
3 3	1	2	7	0.126
5				
3	1	2	8	0.1231
3 3	1	2	9	0.1234
3	1	2	10	0.1246
5				
3	2	1	1	0.1207
3	2	1	2	0.1279
3 3	2	1	3	0.1268
3				
5	2	1	4	0.1222
3 3	2	1	5	0.1244
3	2	1	б	0.1225
3	2	1	7	0.1234
3				
3	2	1	8	0.1244
3 3	2	1	9	0.1207
3	2	1	10	0.1264
2				
3 3	2	2	1	0.1224
3	2	2	2	0.1254
3	2	2	3	0.1237
3	2	2	4	0.1254
5				
3	2	2	5	0.1269
3	2	2	б	0.1236
3	2	2	7	0.1248
3	2	2	8	0.1253
3	2	2	9	0.1252
3	2	2	10	0.1237
2		1	1	
5	3 3			0.1217
3	3	1	2	0.122
3	3	1	3	0.1227
3	3	1	4	0.1202
2	2			
3	3	1	5	0.127
3	3	1	6	0.1224
3	3	1	7	0.1219
2	2	1	8	0.1266
5	5			
3	3	1	9	0.1254
3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	1	10	0.1258
З	3	2	1	0.1236
	с г			
3 3	3	2	2	0.1247
3	3	2	3	0.124
3	3	2	4	0.1235
3	2	2	5	0.124
	2			
3	3	2	б	0.1217

3.5.2.1.	Background and Data
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	3	3	2	7	0.1235
	3	3	2	8	0.1242
	3	3	2	9	0.1247
	3	3	2	10	0.125
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3. Production Process Characterization

3.5. Case Studies

3.5.2. Machine Screw Case Study

3.5.2.2. Box Plots by Factors

Initial Steps The initial step is to plot <u>box plots</u> of the measured diameter for each of the explanatory variables.

Box Plot by The following is a <u>box plot</u> of the diameter by machine. *Machine*



Conclusions From Box Plot We can make the following conclusions from this box plot.

- 1. The location appears to be significantly different for the three machines, with machine 2 having the smallest median diameter and machine 1 having the largest median diameter.
- 2. Machines 1 and 2 have comparable variability while machine 3 has somewhat larger variability.





ConclusionsWe can draw the following conclusion from this box plot. Neither the location nor the spread
seem to differ significantly by day.Plot

Box Plot by The following is a <u>box plot</u> of the time of day.

Time of Day



ConclusionWe can draw the following conclusion from this box plot. Neither the location nor the spreadFrom Boxseem to differ significantly by time of day.Plot

Box Plot by	The following is a <u>box plot</u> of the sample number.
Sample	
Number	


ConclusionWe can draw the following conclusion from this box plot. Although there are some minorFrom Boxdifferences in location and spread between the samples, these differences do not show aPlotnoticeable pattern and do not seem significant.

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<u>Production Process Characterization</u>
 <u>Case Studies</u>
 <u>S.2.</u> Machine Screw Case Study

3.5.2.3. Analysis of Variance

Analysis of Variance using All Factors We can confirm our interpretation of the box plots by running an analysis of variance. Dataplot generated the following analysis of variance output when all four factors were included.

NUMBER OF	OBSERVATIONS	=	180
NUMBER OF	FACTORS	=	4
NUMBER OF	LEVELS FOR FACTOR 1	=	3
NUMBER OF	LEVELS FOR FACTOR 2	=	3
NUMBER OF	LEVELS FOR FACTOR 3	=	2
NUMBER OF	LEVELS FOR FACTOR 4	=	10
BALANCED	CASE		
RESIDUAL	STANDARD DEVIATION	=	0.13743976597E-02
RESIDUAL	DEGREES OF FREEDOM	=	165
NO REPLIC			
NUMBER OF	DISTINCT CELLS	=	180

* * * * * * * * * * * * * * * * *

DF SUM	OF SQUARES	MEAN SQUARE	F STATISTIC	F CDF	SIG
179	0.000437	0.000002			
2 2 1 9	0.000111 0.000004 0.000002 0.000009	0.000055 0.000002 0.000002 0.000002 0.000001	29.3159 0.9884 1.2478 0.5205	100.000% 62.565% 73.441% 14.172%	**
011101110	2212101		139766		
	179 2 2 1 9 165 STANDARD	179 0.000437 2 0.000111 2 0.000004 1 0.000002 9 0.000009	179 0.000437 0.000002 2 0.0000111 0.0000055 2 0.000004 0.000002 1 0.000002 0.000002 9 0.000009 0.000001 165 0.000312 0.000002 STANDARD DEVIATION = 0.001374	179 0.000437 0.000002 2 0.000111 0.000055 29.3159 2 0.000004 0.000002 0.9884 1 0.000002 0.9884 9 0.000002 0.000002 165 0.000312 0.000002 STANDARD DEVIATION = 0.00137439766	179 0.000437 0.000002 2 0.000111 0.000055 29.3159 100.000% 2 0.000004 0.000002 0.9884 62.565% 1 0.000002 0.000002 1.2478 73.441% 9 0.000009 0.000001 0.5205 14.172% 165 0.000312 0.000002 0.00137439766

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	* *	* * * * * * * * * * * * *	*	
	*	ESTIMATION	*	
	* *	* * * * * * * * * * * * *	*	
GRAND MI	EAN	=	0.	.12395893037E+00
GRAND ST	TANDARD DEVIAT	ION =	0.	.15631503193E-02

	LEVEL-ID	NI	MEAN	EFFECT	SD(EFFECT)
FACTOR 1	1.00000	60.	0.12489	0.00093	0.00014
	2.00000	60.	0.12297	-0.00099	0.00014
	3.00000	60.	0.12402	0.00006	0.00014
FACTOR 2	1.00000	60.	0.12409	0.00013	0.00014
	2.00000	60.	0.12403	0.00007	0.00014
	3.00000	60.	0.12376	-0.00020	0.00014
FACTOR 3	1.00000	90.	0.12384	-0.00011	0.00010
	2.00000	90.	0.12407	0.00011	0.00010
FACTOR 4	1.00000	18.	0.12371	-0.00025	0.00031
	2.00000	18.	0.12405	0.00009	0.00031
	3.00000	18.	0.12398	0.00002	0.00031
	4.00000	18.	0.12382	-0.00014	0.00031
	5.00000	18.	0.12426	0.00030	0.00031
	6.00000	18.	0.12379	-0.00016	0.00031
	7.00000	18.	0.12406	0.00010	0.00031
	8.00000	18.	0.12376	-0.00020	0.00031
	9.00000	18.	0.12376	-0.00020	0.00031
	10.00000	18.	0.12440	0.00044	0.00031

MODEL

RESIDUAL STANDARD DEVIATION

CONSTANT	ONLY	0.0015631503
CONSTANT &	FACTOR 1 ONLY	0.0013584237
CONSTANT &	FACTOR 2 ONLY	0.0015652323
CONSTANT &	FACTOR 3 ONLY	0.0015633047
CONSTANT &	FACTOR 4 ONLY	0.0015876852
CONSTANT &	ALL 4 FACTORS	0.0013743977

Interpretation of ANOVA Output The first thing to note is that Dataplot fits an overall mean when performing the ANOVA. That is, it fits the model

$$Y_{ijklm} = \mu + lpha_i + eta_j + au_k + \phi_l + \epsilon_{ijklm}$$

as opposed to the model

$$Y_{ijklm} = A_i + B_j + C_k + D_l + \epsilon_{ijklm}$$

These models are mathematically equivalent. The effect estimates in the first model are relative to the overall mean. The effect estimates for the second model can be obtained by simply adding the overall mean to effect estimates from the first model.

We are primarily interested in identifying the significant factors. The

last column of the ANOVA table prints a "**" for statistically significant factors. Only factor 1 (the machine) is statistically significant. This confirms what the box plots in the previous section had indicated graphically.

Analysis of
VarianceThe previous analysis of variance indicated that only the machine
factor was statistically significant. The following shows the ANOVA
output using only the machine factor.MachineMachine

NUMBER OF OBSERVATIONS	=	180
NUMBER OF FACTORS	=	1
NUMBER OF LEVELS FOR FACTOR 1	=	3
BALANCED CASE		
RESIDUAL STANDARD DEVIATION	=	0.13584237313E-02
RESIDUAL DEGREES OF FREEDOM	=	177
REPLICATION CASE		
REPLICATION STANDARD DEVIATION	=	0.13584237313E-02
REPLICATION DEGREES OF FREEDOM	=	177
NUMBER OF DISTINCT CELLS	=	3

* * * * * * * * * * * * * * * * * *

SOURCE	DF SUM OF SQUAR	ES MEA	AN SQUARE	F STATISTIC	F CDF	SIG
TOTAL (CORRECTED)	179 0.0004	37	0.000002			
FACTOR 1	2 0.0001	.11	0.000055	30.0094	100.000%	**
RESIDUAL	177 0.0003	27	0.000002			
RESIDUAL REPLICATION	STANDARD DEVIATIO DEGREES OF FREEDO STANDARD DEVIATIO DEGREES OF FREEDO	0M = 0N =	177			
	********** * ESTIMAT ********	'ION *				
GRAND MEAN GRAND STAND	ARD DEVIATION	= =	0.12395893 0.15631503			

	LEVEL-ID	NI	MEAN	EFFECT	SD(EFFECT)	
FACTOR 1 	1.00000 2.00000 3.00000	60. 60. 60.	0.12489 0.12297 0.12402	0.00093 -0.00099 0.00006	0.00014 0.00014 0.00014	
MODE	L	RESIDUAL STANDARD DEVIATION				
	ONT	37	0 00150	21502		

CONSTANT				ONLY	0.0015631503
CONSTANT	&	FACTOR	1	ONLY	0.0013584237

Interpretation of ANOVA

At this stage, we are interested in the effect estimates for the machine variable. These can be summarized in the following table.

Output

Means for Oneway Anova

Level	Number	Mean	Standard Error	Lower 95% CI	Upper 95% CI
1	60	0.124887	0.00018	0.12454	0.12523
2	60	0.122968	0.00018	0.12262	0.12331
3	60	0.124022	0.00018	0.12368	0.12437

The Dataplot macro file shows the computations required to go from the Dataplot ANOVA output to the numbers in the above table.

Model As a final step, we <u>validate the model</u> by generating a <u>4-plot</u> of the residuals.

Validation



The 4-plot does not indicate any significant problems with the ANOVA model.



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3.5.2.4. Throughput

Summary of Throughput The throughput is summarized in the following table (this was part of the original data collection, not the result of analysis).

Machine	Day 1	Day 2	Day 3
1	576	604	583
2	657	604	586
3	510	546	571

We can show the throughput graphically.

This table shows that machine 3 had significantly lower throughput.

Graphical Representation of Throughput



The graph clearly shows the lower throughput for machine 3.

Analysis of We can confirm the statistical significance of the lower throughput of machine 3 by running an Variance for analysis of variance. Throughput **** 1-WAY ANALYSIS OF VARIANCE ** NUMBER OF OBSERVATIONS NUMBER OF FACTORS = 9 = 1 3 NUMBER OF LEVELS FOR FACTOR 1 = BALANCED CASE RESIDUAL STANDARD DEVIATION = 0.28953985214E+02 RESIDUAL DEGREES OF FREEDOM = 6 б REPLICATION CASE REPLICATION STANDARD DEVIATION = 0.28953985214E+02 REPLICATION DEGREES OF FREEDOM = 6 NUMBER OF DISTINCT CELLS = 3 * * * * * * * * * * * * * * * * * * ANOVA TABLE * ************ DF SUM OF SQUARES MEAN SQUARE F STATISTIC F CDF SIG SOURCE _____ TOTAL (CORRECTED) 8 13246.888672 1655.861084 _____ FACTOR 1 2 8216.898438 4108.449219 4.9007 94.525% _____ RESIDUAL 6 5030.000000 838.33313 RESIDUALSTANDARD DEVIATION =28.95398521423RESIDUALDEGREES OF FREEDOM =6 REPLICATION STANDARD DEVIATION =6REPLICATION DEGREES OF FREEDOM =6 * * * * * * * * * * * * * * * * * ESTIMATION * * * * * * * * * * * * * * * * * = 0.58188891602E+03 GRAND MEAN = 0.40692272186E+02 GRAND STANDARD DEVIATION LEVEL-ID NI MEAN EFFECT SD(EFFECT) _____ FACTOR 1-- 1.00000 3. 587.66669 5.77777 13.64904 2.00000 3. 615.66669 33.77777 13.64904 ___

_ _

_	3.00000	3.	542.33331	-39.55560	13.64904

MODEL		RESIDUAL STANDARD DEVIATION
CONSTANT	ONLY	40.6922721863
CONSTANT & FACTOR	1 ONLY	28.9539852142

Interpretation We summarize the effect estimates in the following table.

of ANOVA Output

Means for Oneway Anova

Level	Number	Mean	Standard Error	Lower 95%	Upper 95%
				CI	CI
1	3	587.667	16.717	546.76	628.57
2	3	615.667	16.717	574.76	656.57
3	3	542.33	16.717	501.43	583.24

The <u>Dataplot macro file</u> shows the computations required to go from the Dataplot ANOVA output to the numbers in the above table.

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3.5.2.5. Final Conclusions

Final Conclusions The analysis shows that machines 1 and 2 had about the same variablity but significantly different locations. The throughput for machine 2 was also higher with greater variability than for machine 1. An interview with the operator revealed that he realized the second machine was not set correctly. However, he did not want to change the settings because he knew a study was being conducted and was afraid he might impact the results by making changes. Machine 3 had significantly more variation and lower throughput. The operator indicated that the machine had to be taken down several times for minor repairs. Given the preceeding analysis results, the team recommended replacing machine 3.





3. <u>Production Process Characterization</u> 3.5. Case Studies

3.5.2. Machine Screw Case Study

3.5.2.6. Work This Example Yourself

<u>View</u>
<u>Dataplot</u>
<u>Macro for</u>
<u>this Case</u>
<u>Study</u>

This page allows you to repeat the analysis outlined in the case study description on the previous page using <u>Dataplot</u>, if you have <u>downloaded and installed it</u>. Output from each analysis step below will be displayed in one or more of the Dataplot windows. The four main windows are the Output window, the Graphics window, the Command History window and the Data Sheet window. Across the top of the main windows there are menus for executing Dataplot commands. Across the bottom is a command entry window where commands can be typed in.

Data Analysis Steps	Results and Conclusions
Click on the links below to start Dataplot and run this case study yourself. Each step may use results from previous steps, so please be patient. Wait until the software verifies that the current step is complete before clicking on the next step.	The links in this column will connect you with more detailed information about each analysis step from the case study description.
1. Get set up and started.	
<u> 1. Read in the data.</u>	<u>1. You have read 5 columns of numbers</u> <u>into Dataplot, variables machine,</u> <u>day, time, sample, and diameter.</u>

2. Box Plots by Factor Variables 1. Generate a box plot by machine.	<u>1. The box plot shows significant</u> variation for both location and spread.
<u>2. Generate a box plot by day.</u>	2. The box plot shows no significant location or spread effects for day.
<u>3. Generate a box plot by time of</u> <u>day.</u>	<u>3. The box plot shows no significant</u> <u>location or spread effects for</u> <u>time of day.</u>
<u>4. Generate a box plot by</u> <u>sample.</u>	<u>4. The box plot shows no significant</u> <u>location or spread effects for</u> <u>sample.</u>
3. Analysis of Variance	
<u> 1. Perform an analysis of variance</u> <u> with all factors.</u>	1. The analysis of variance shows that only the machine factor is statistically significant.
2. Perform an analysis of variance with only the machine factor.	2. The analysis of variance shows the overall mean and the effect estimates for the levels of the machine variable.
<u>3. Perform model validation by</u> <u>generating a 4-plot of the</u> <u>residuals.</u>	<u>3. The 4-plot of the residuals does</u> <u>not indicate any significant</u> <u>problems with the model.</u>

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4. Graph of Throughput		
<u> 1. Generate a graph of the</u> <u> throughput.</u>	<u>1. The graph shows the throughput</u> <u>for machine 3 is lower than</u> <u>the other machines.</u>	
<u>2. Perform an analysis of</u> <u>variance of the throughput.</u>	2. The effect estimates from the ANIVA are given.	
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3.6. References

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